

# Towards Characterization of the First Stars and Galaxies (and Beyond) with Low-frequency Radio Observations

Piyanat (Boom) Kittiwisit

Arizona State University (ASU), University of KwaZulu-Natal (UKZN)

Collaborators

ASU (USA): Judd Bowman, Daniel Jacobs, Adam Beardsley, Steven Murray

NRAO (USA): Nithya Thyagarajan, UKZN (SA): Yin-Zhe Ma

NARIT, July 19, 2019

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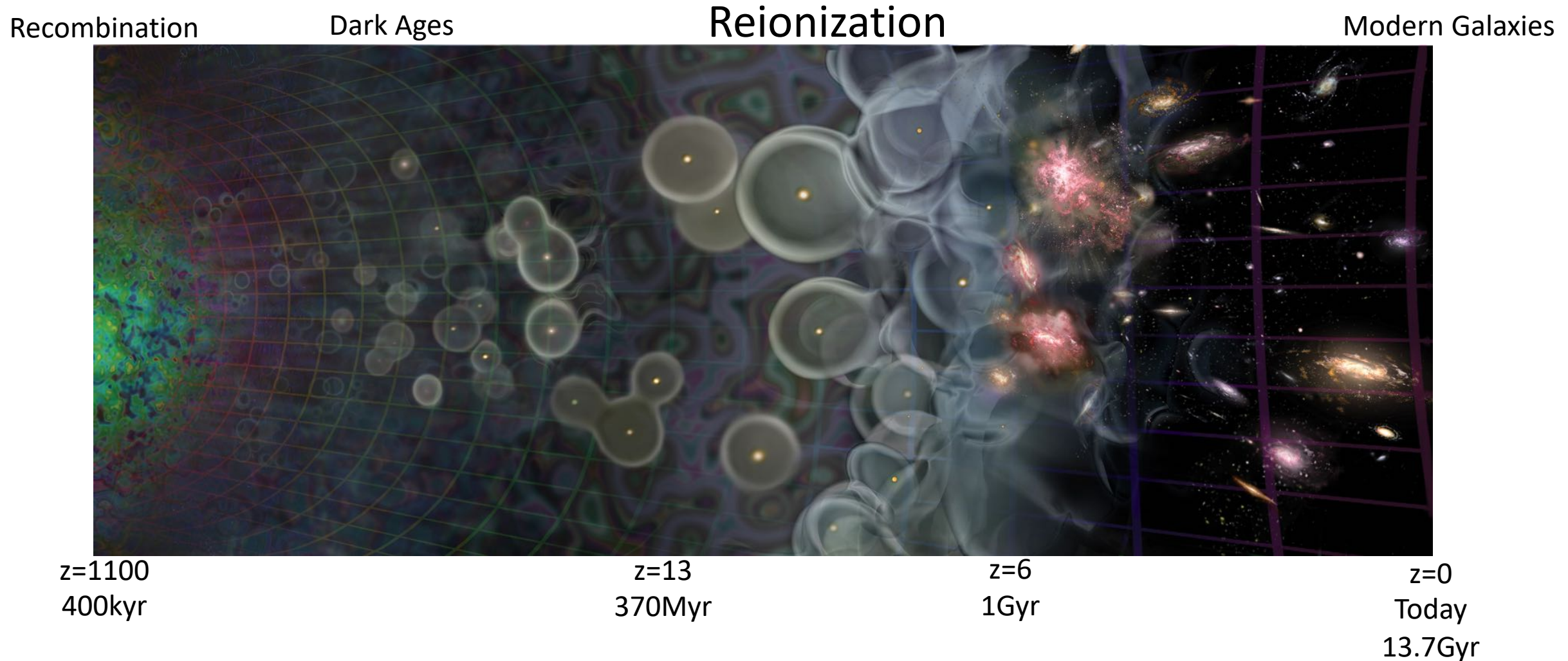
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NARIT, July 19, 2019

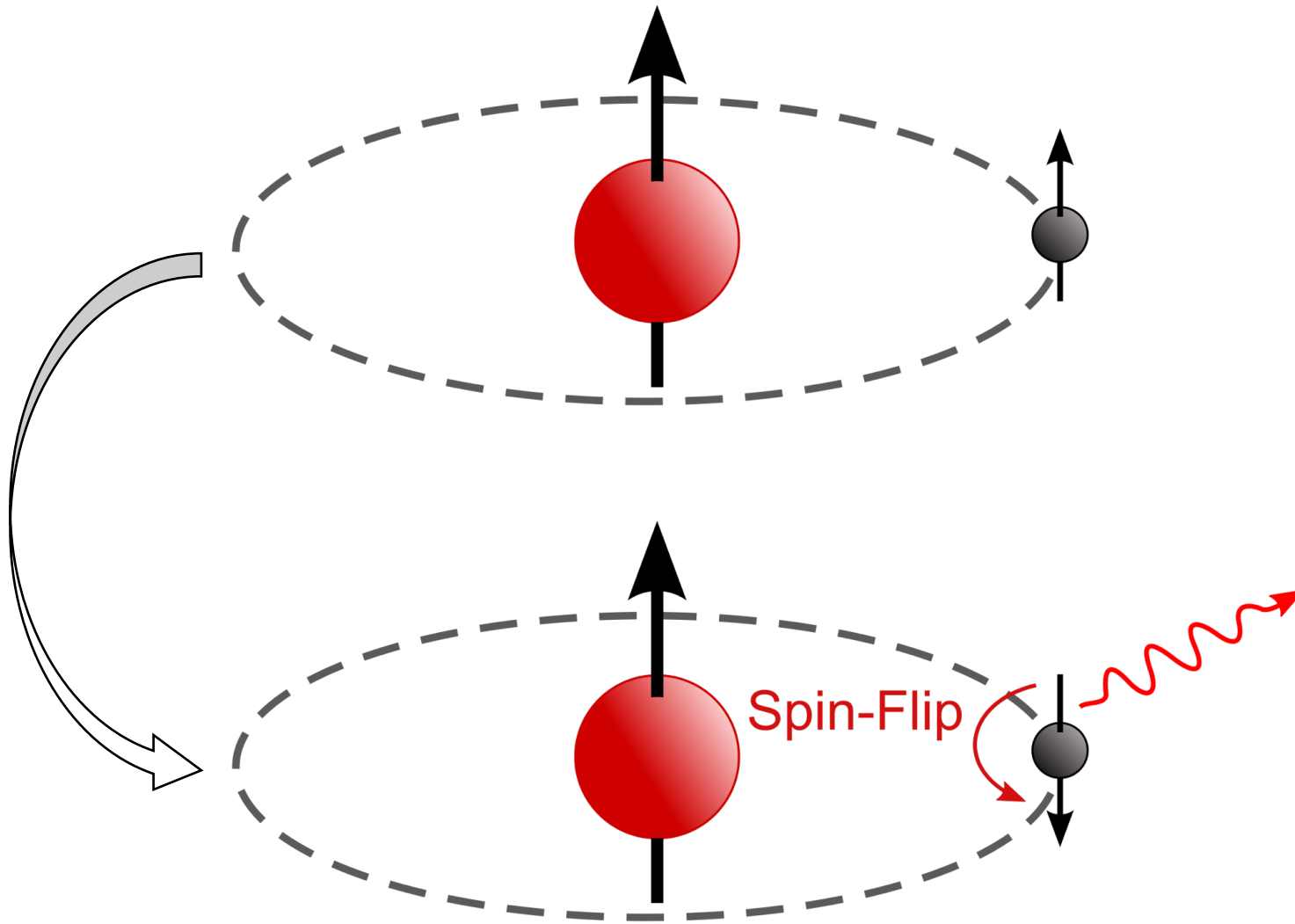
# Outline

- Part I – Overview of Low-frequency Cosmology
- Part II – My Work on Statistical Analysis of Low-frequency Cosmology Data
- Part III – Beyond Cosmology – Examples of Space Weather Physics from Low-frequency Radio Observations

# When and how were the first stars and galaxies formed and evolved into modern large-scale structure?



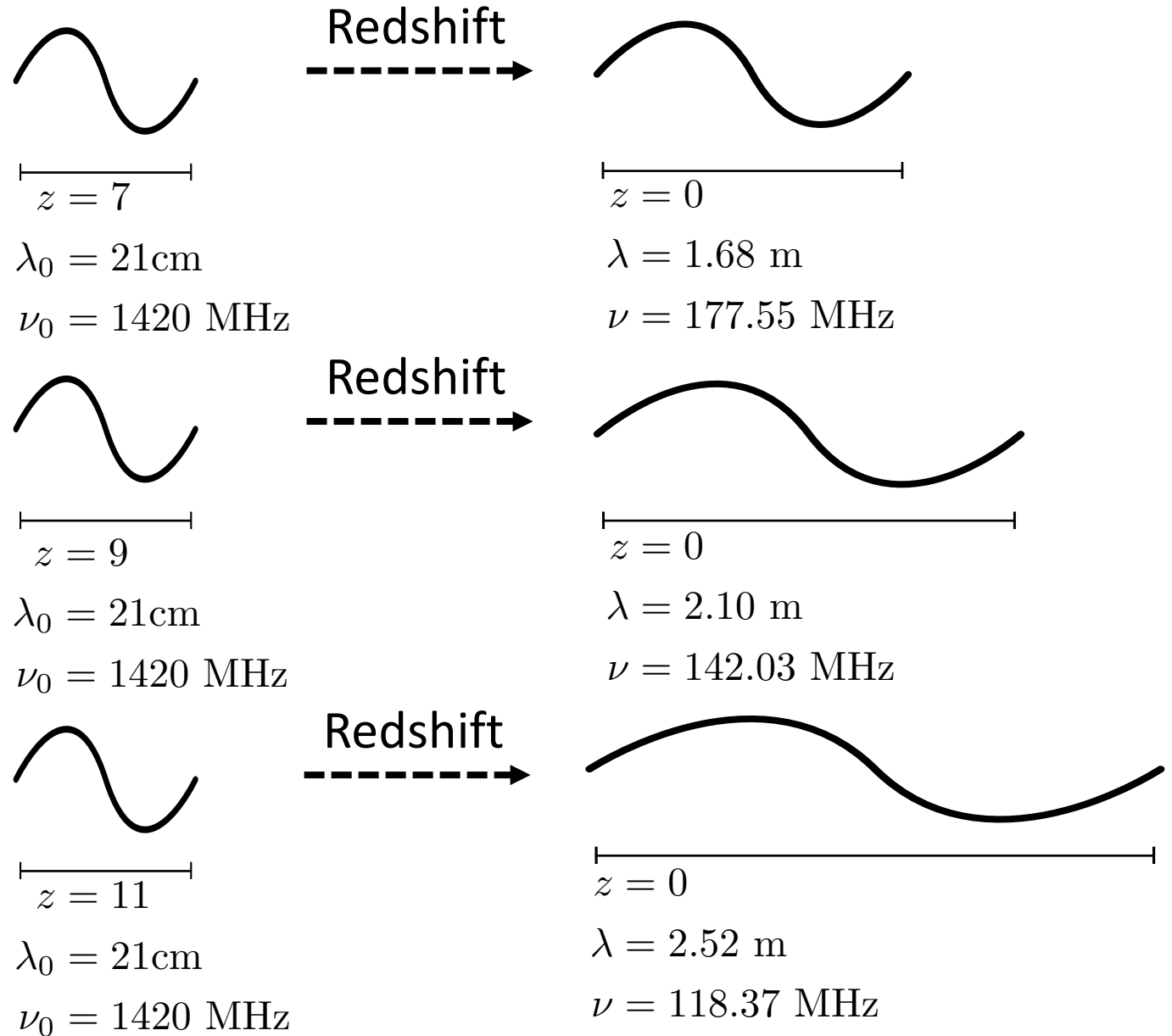
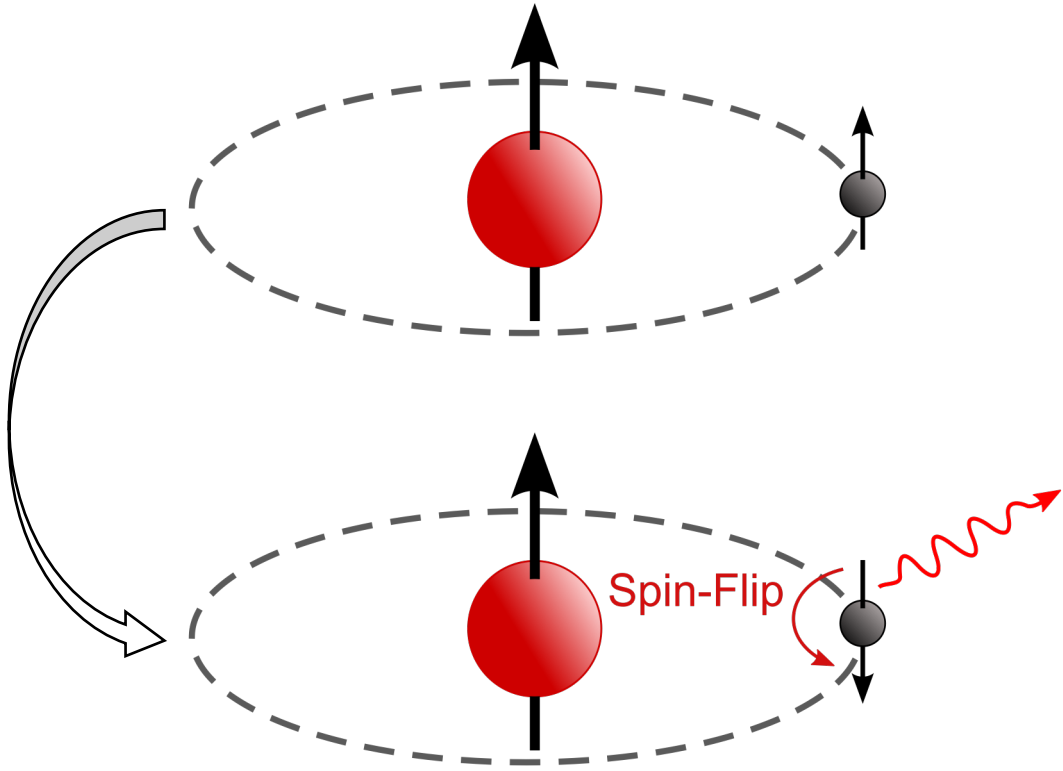
# 21 cm lines can be used to probe reionization



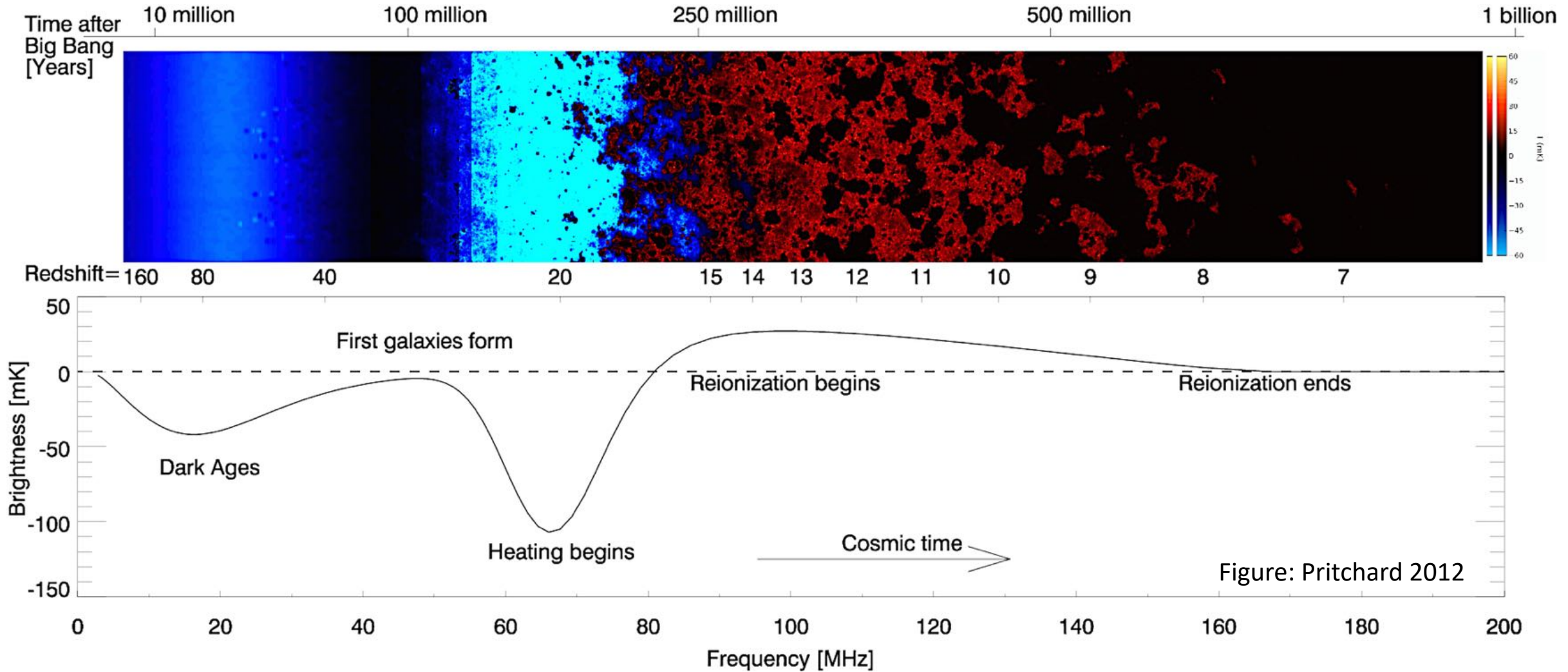
$$\lambda_0 = 21\text{cm}$$

$$\nu_0 = 1420\text{ MHz}$$

# 21 cm lines can be used to probe reionization



# 21 cm Brightness Temperature Fluctuations



$$\delta T_b(r_{\parallel}) \approx 9x_{HI}(r_{\parallel})(1 + \delta(r_{\parallel}))(1 + z)^{1/2} \left[ 1 - \frac{T_{\gamma}}{T_S} \right] \left[ \frac{H(z)/(1+z)}{dv_{\parallel}/dr_{\parallel}} \right] \text{ mK.}$$

See Madau et al. 1997 for derivation

# Currently Operating and Future Experiments



MWA in AUS



LOFAR in NE and EU



GMRT in India



HERA in South Africa



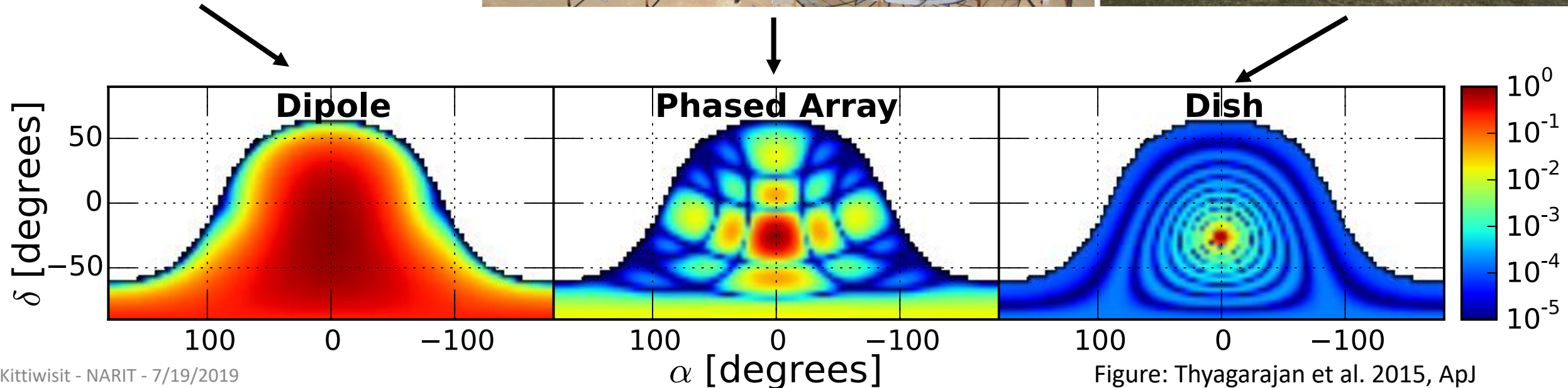
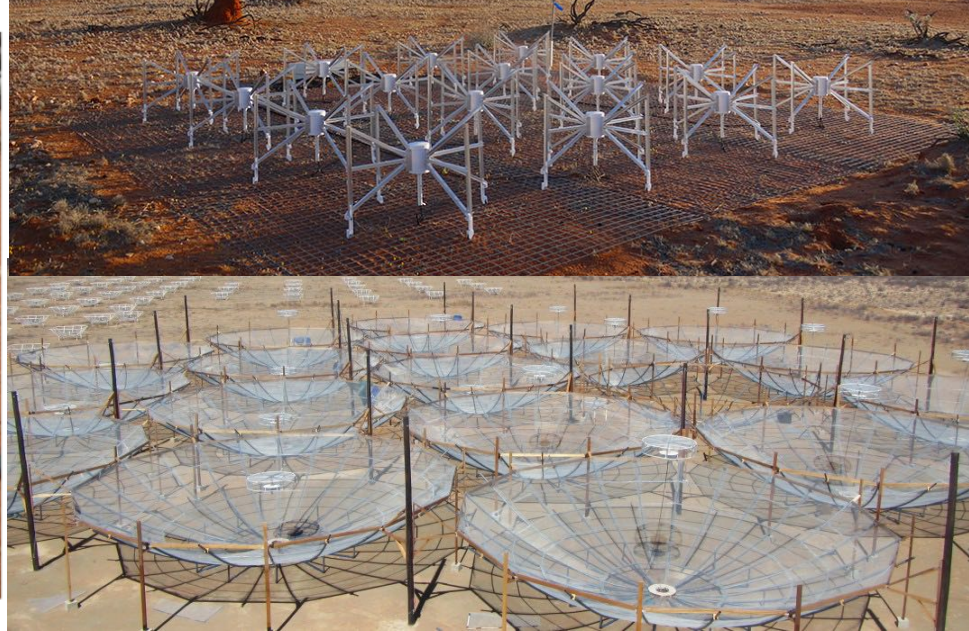
SKA to be in SA and AUS



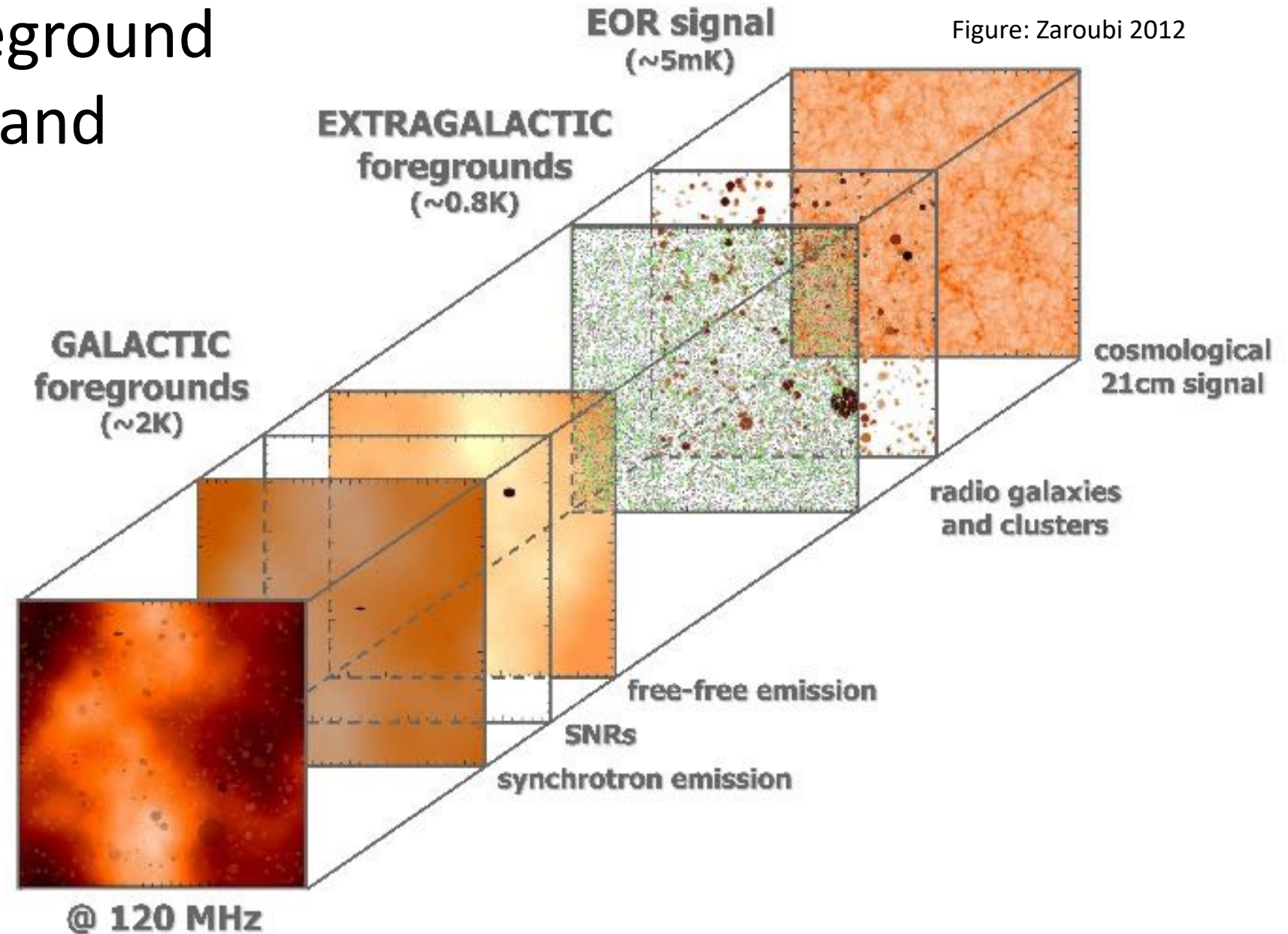
LWA in US



# Challenges #1: Telescope response is complex



# Challenges #2: Foreground is extremely bright and must be mitigated



# Current detection efforts are statistical primarily through 21 cm power spectrum

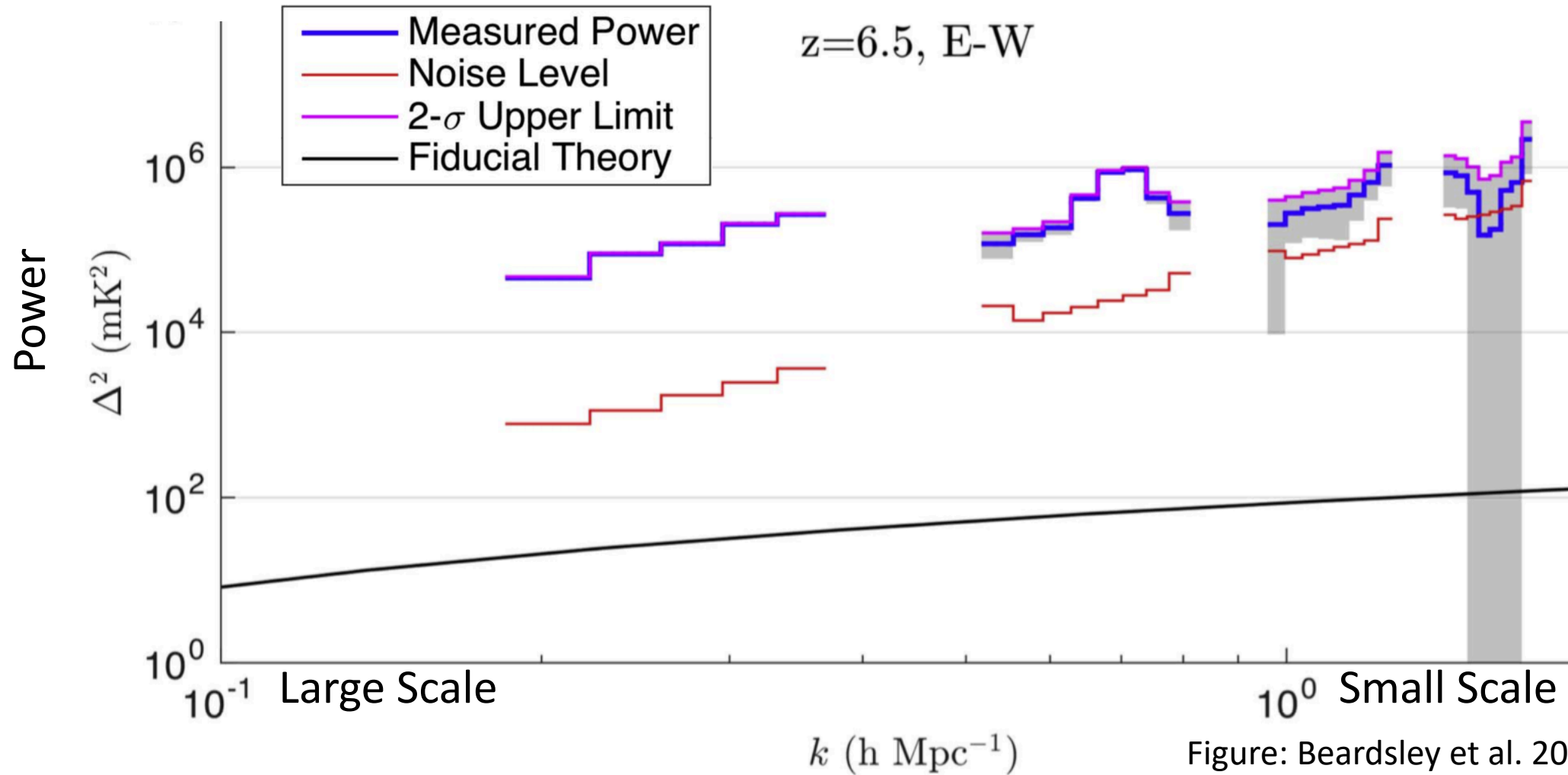
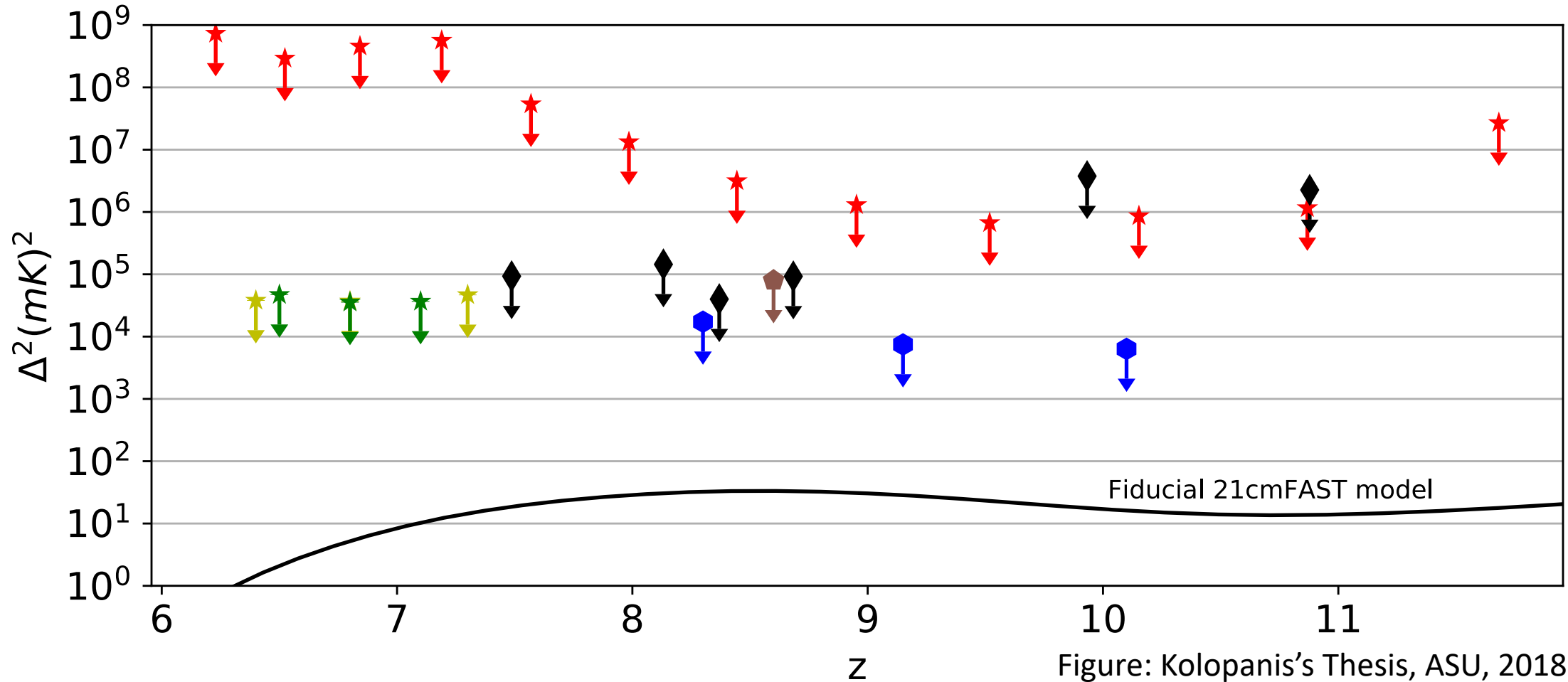


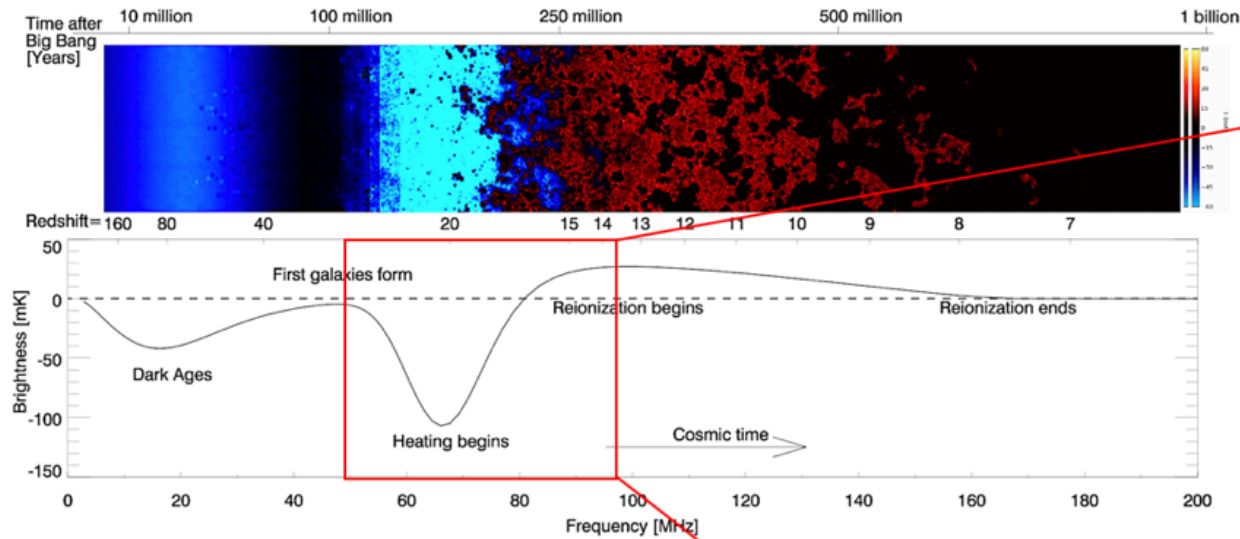
Figure: Beardsley et al. 2016, MNRAS

# Current State of the Field - Averaged Power Spectrum

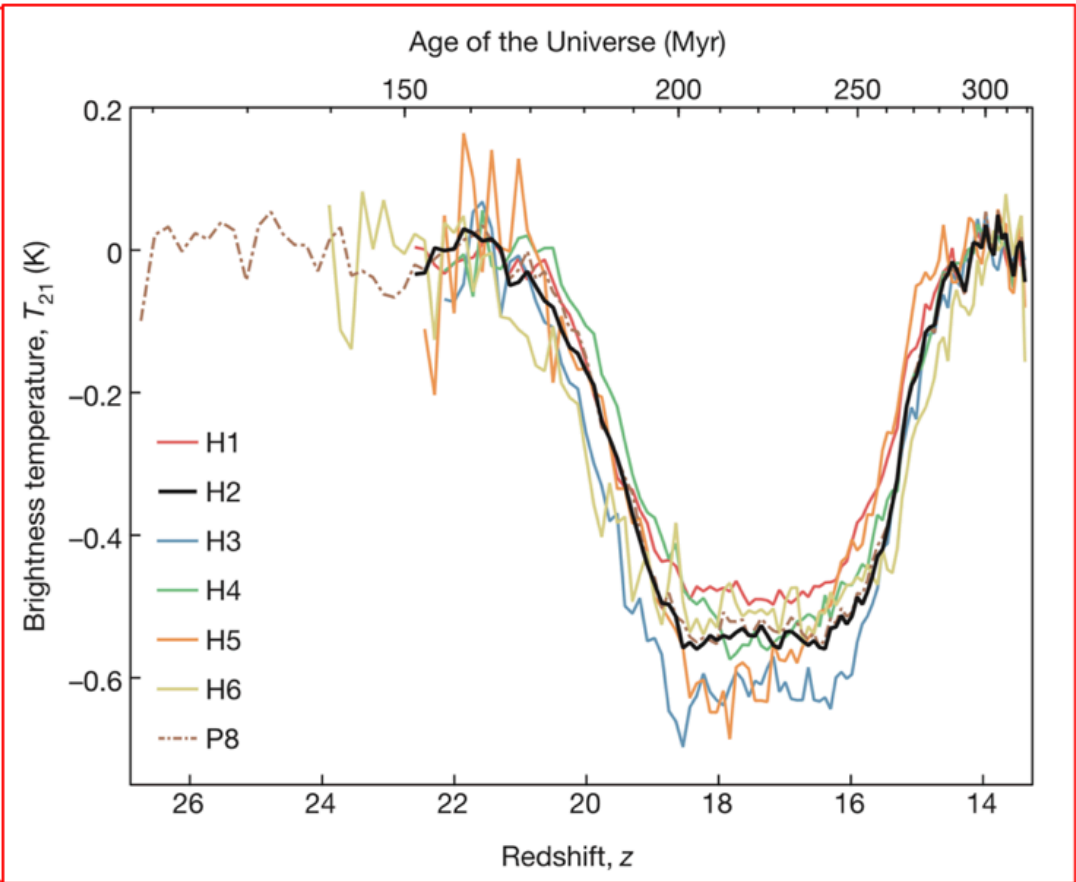


- ★ Dillon, 2014
- ★ Dillon, 2015
- ★ Beardsley, 2016
- ⬢ Patil, 2017
- ⬢ Paciga, 2013
- ⬢ Kolopanis, in prep.

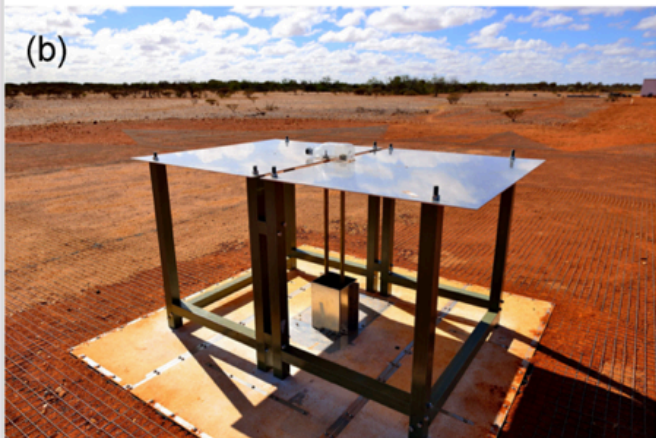
# Global 21 cm experiments aim to measure the sky-averaged 21 cm spectrum from EoR/CD



## Experiment to Detect the Global Epoch of Reionization Signature (EDGES)



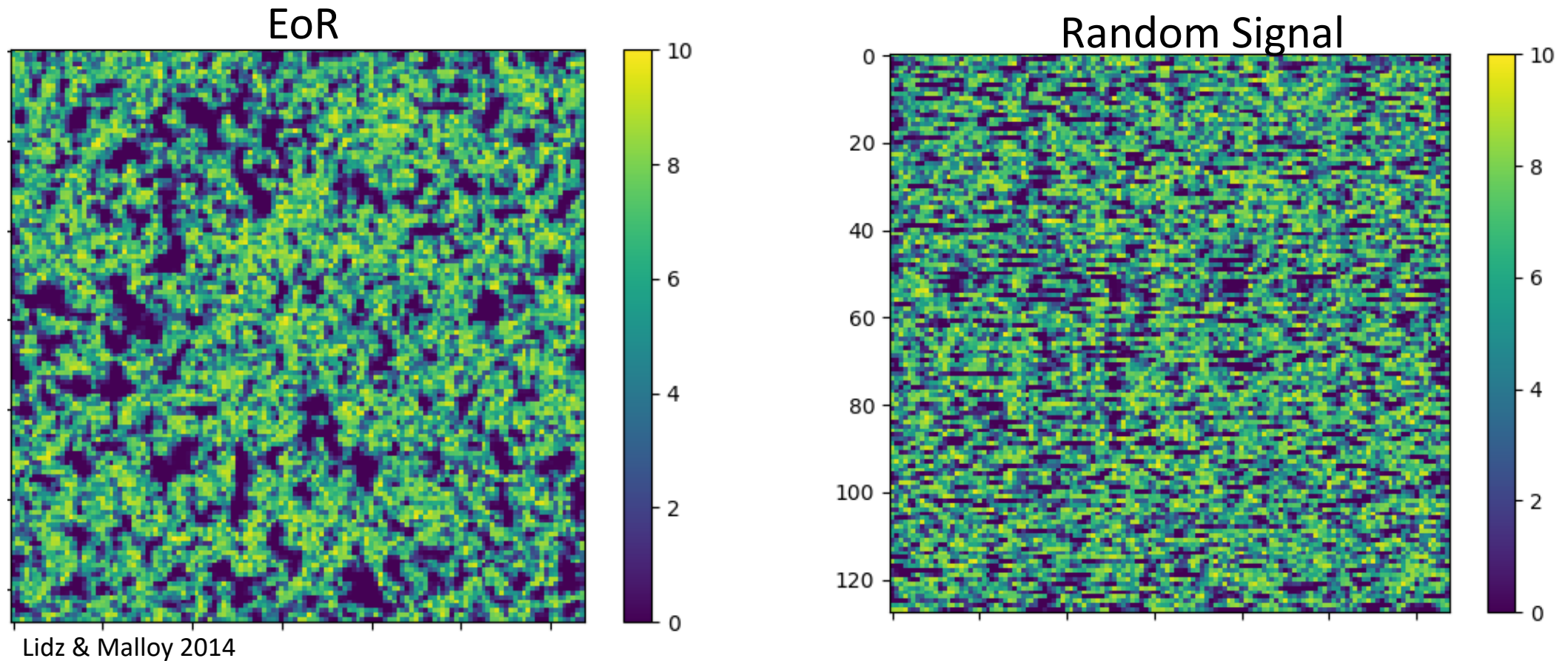
Bowman et al. 2018, Nature, 555, 67–70



# Part I - Summary

- 21 cm lines can be used to probe neutral hydrogen gas during reionization and Cosmic Dawn eras to study formation and evolution of the first stars and galaxies
- It can be done with a radio interferometer in meter wavelengths
- It is very challenging due to complex instruments and bright foreground
- Statistical analysis will be important for the next decade

A power spectrum can only describes a Gaussian signal  
- EoR is not Gaussian



Random signal with the same variance as the EoR signal will have the same power spectrum

# Probability Distribution Function (PDF) and One-point statistics

- PDF: histogram of a map normalized to integral of one
- Variance (2<sup>nd</sup> order) describes the spread
- Skewness (3<sup>rd</sup> order) describes the symmetry
  - Positive = tail above mean
  - Negative = tail below mean
- Kurtosis (4<sup>th</sup> order) describe tailedness
  - Positive = more tails
  - Negative = less tails
- A perfect Gaussian has zero skewness and kurtosis

- Mathematically, one-point statistics are standardization of statistical moments

$$m_p = \frac{1}{N} \sum_{i=0}^N (x - \bar{x})^p$$

$$\text{variance} = m_2$$

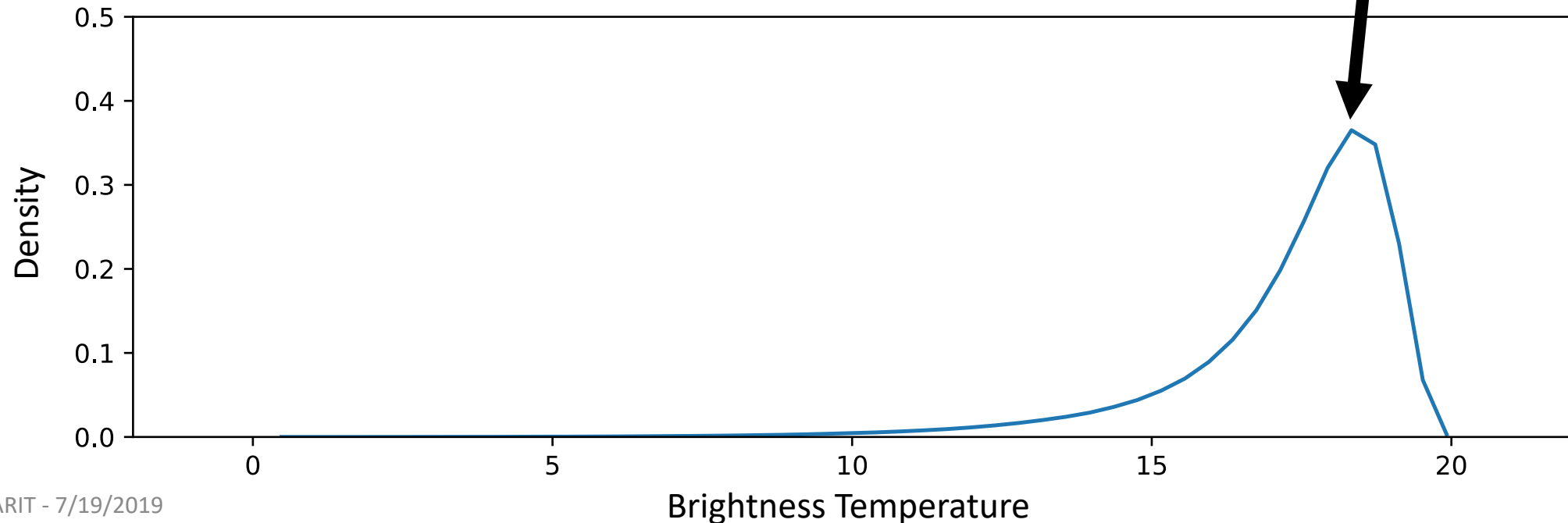
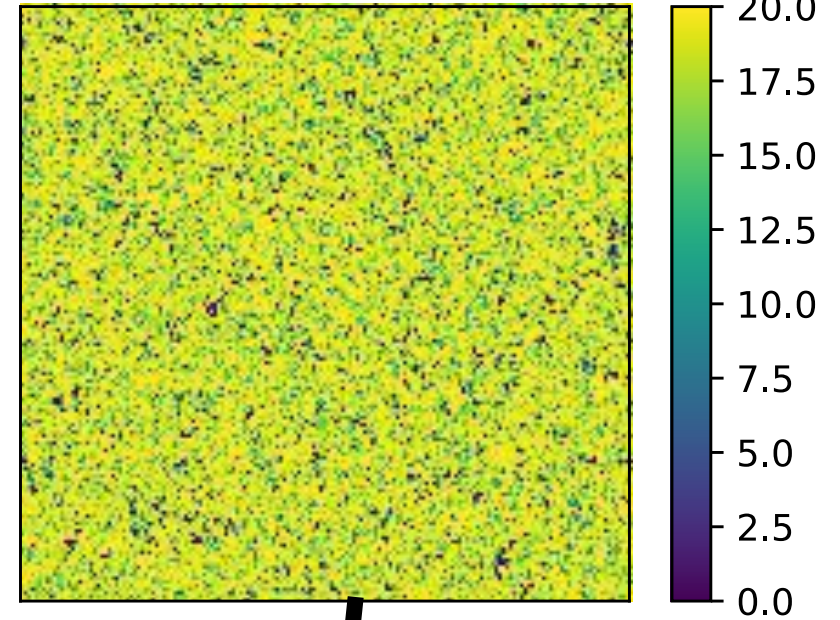
$$\text{skewness} = \frac{m_3}{m_2^{(3/2)}}$$

$$\text{kurtosis} = \frac{m_4}{m_2^2} - 3$$



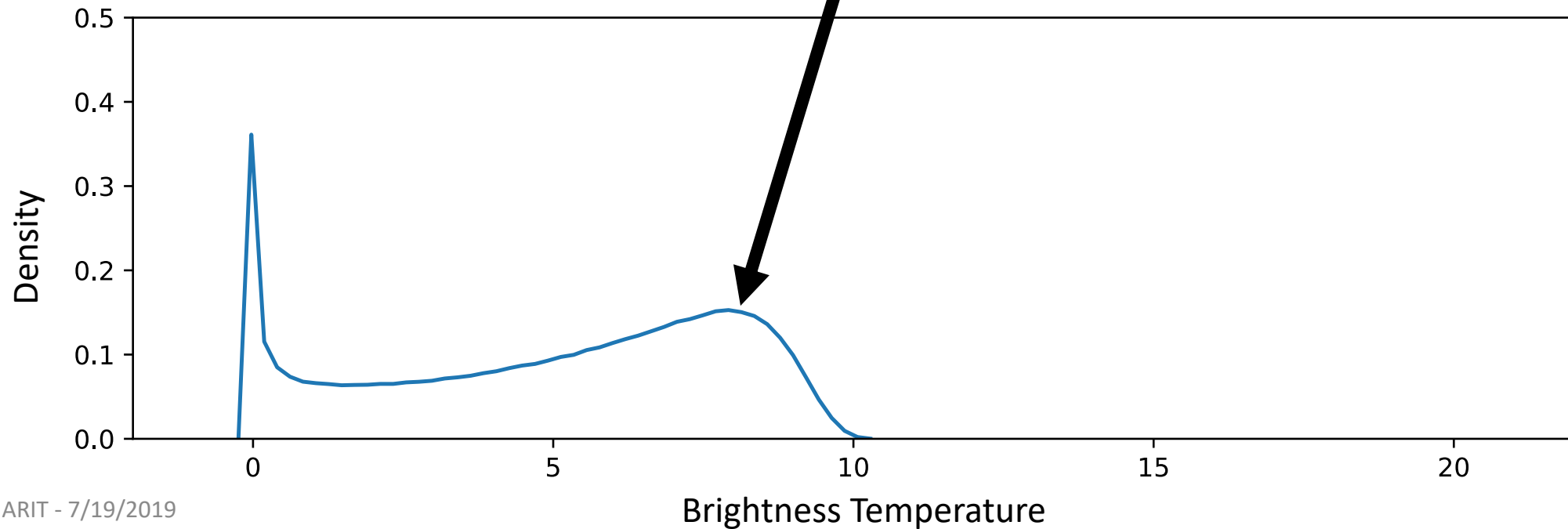
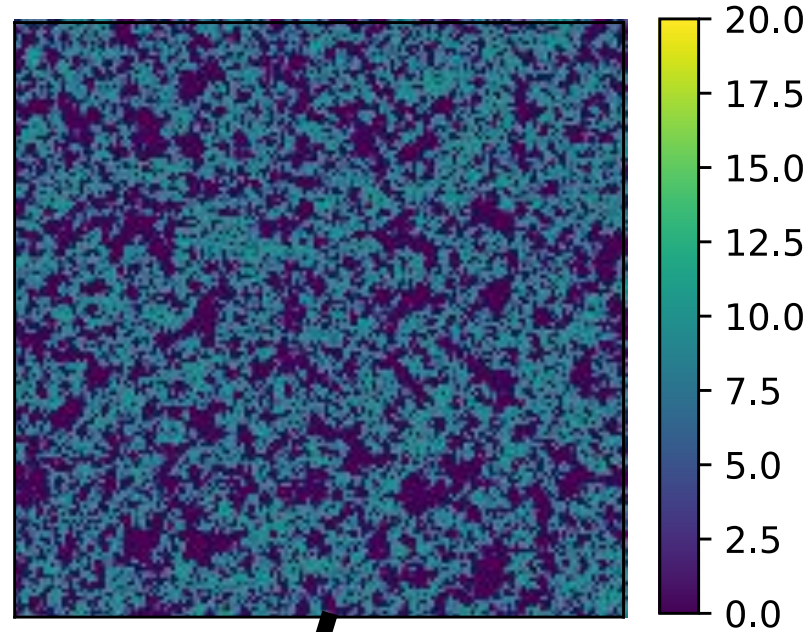
## 30% Ionized

- Gaussian-like peak with a long left tail
- Negative skewness
- Positive kurtosis

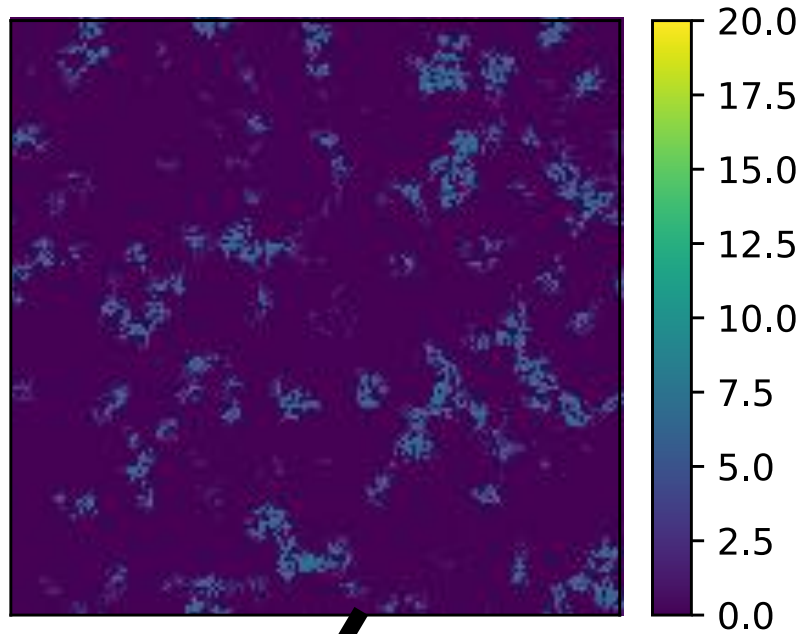


## 70% Ionized

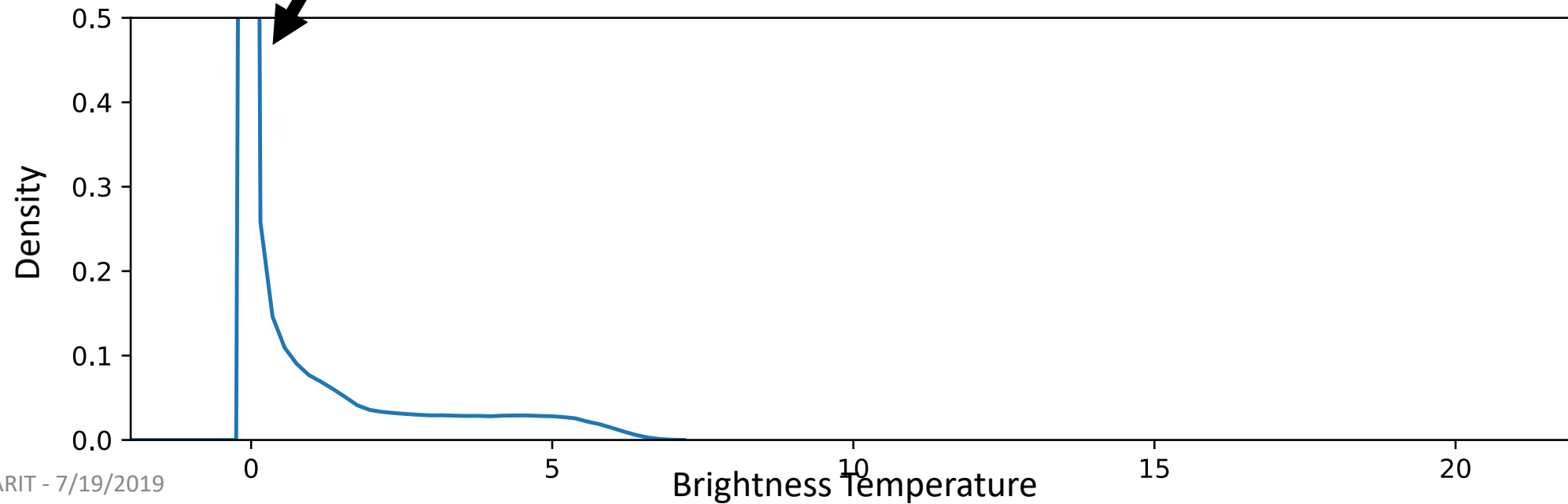
- Bi-modal PDF (twin-peaks PDF)
- High variance
- Negative kurtosis

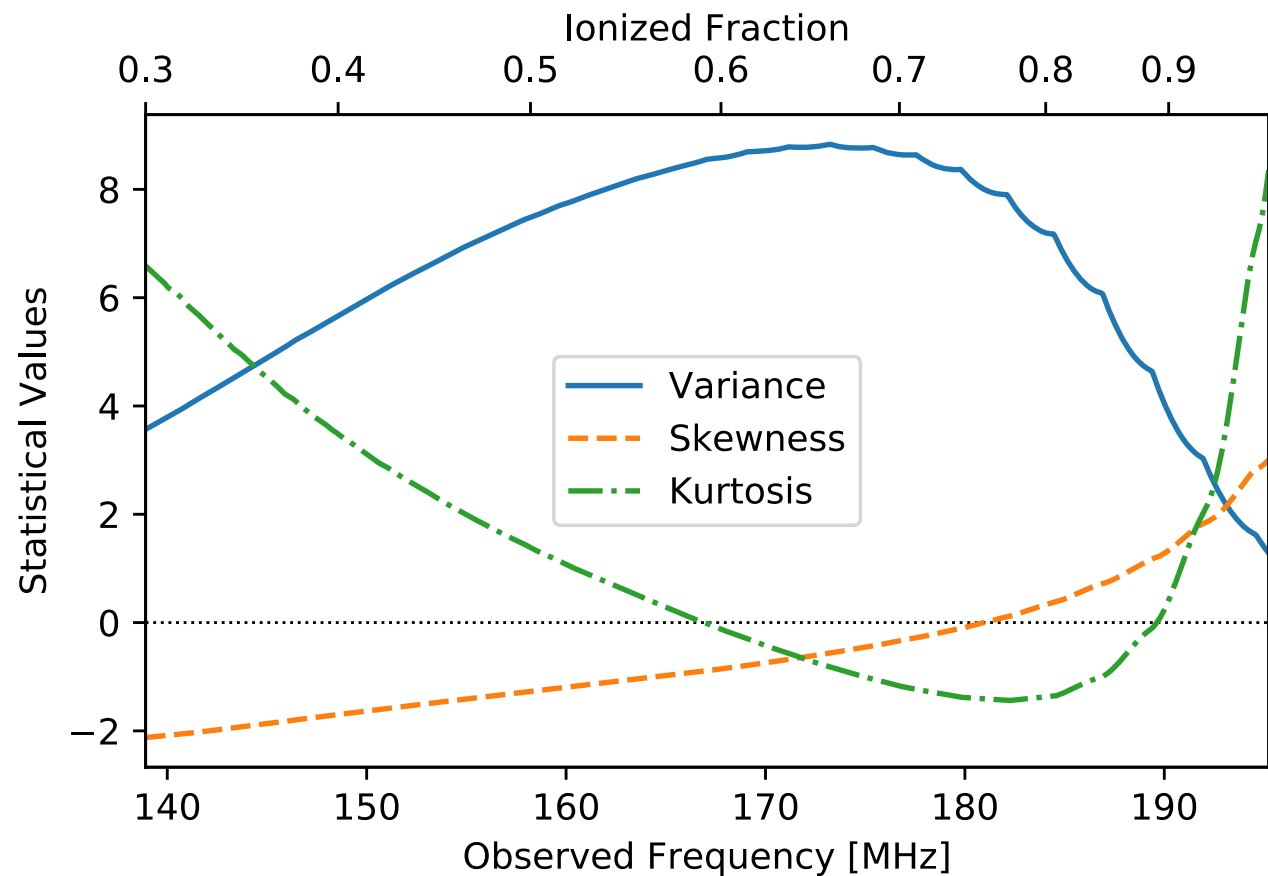
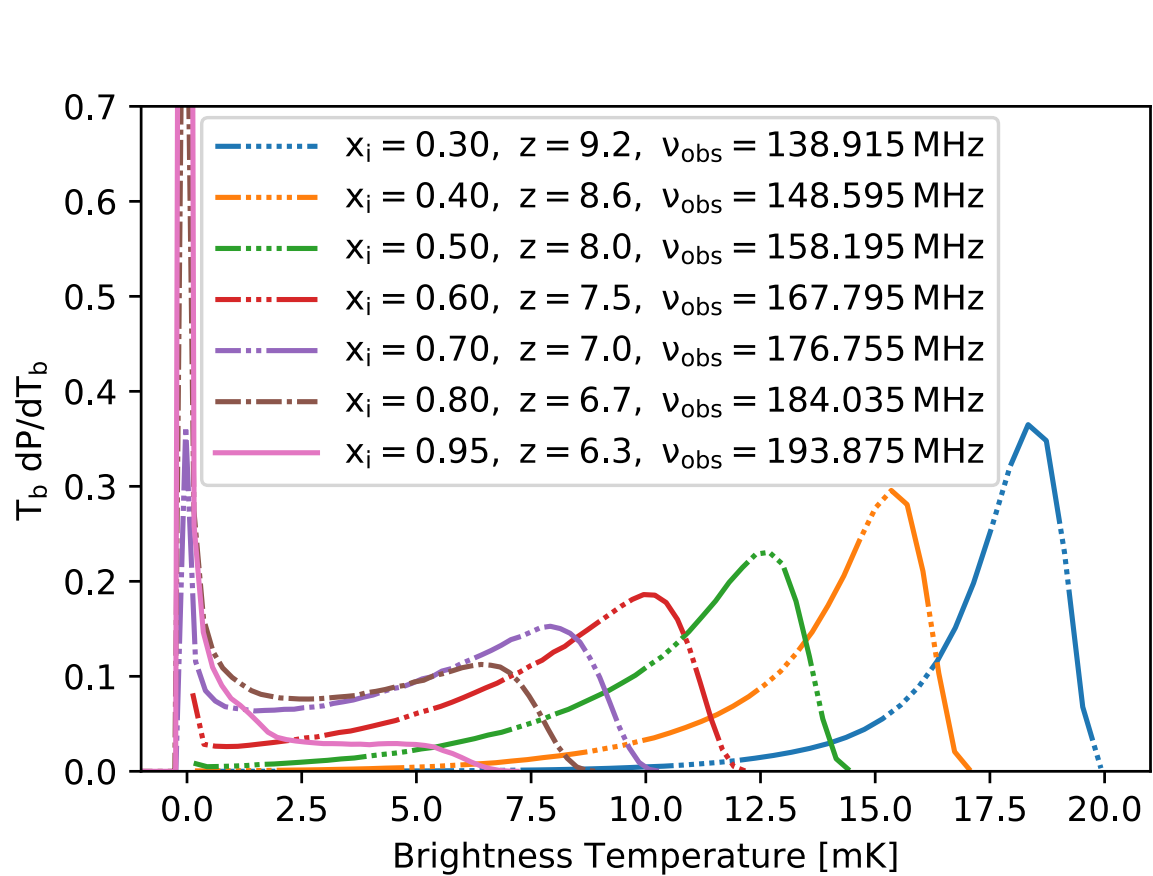
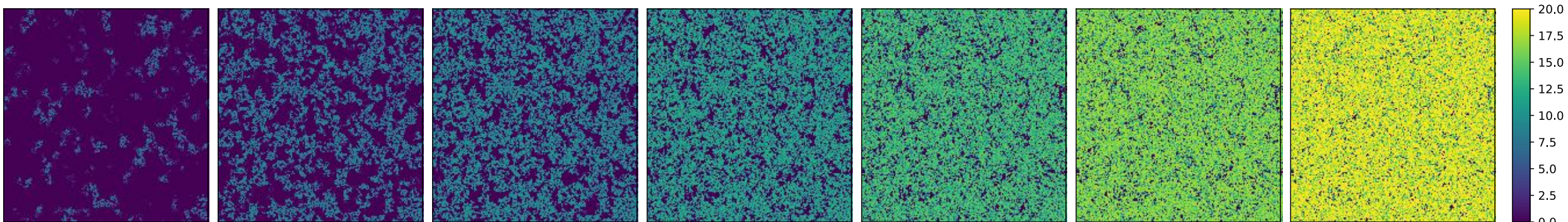


# 95% Ionized



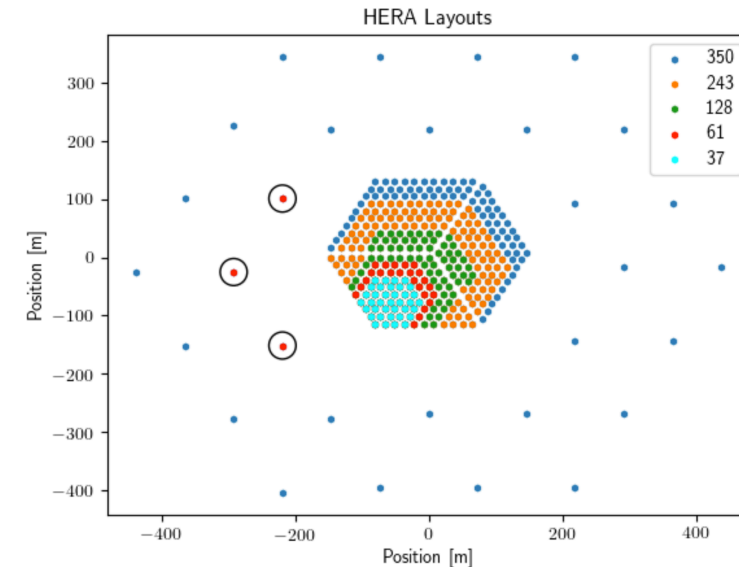
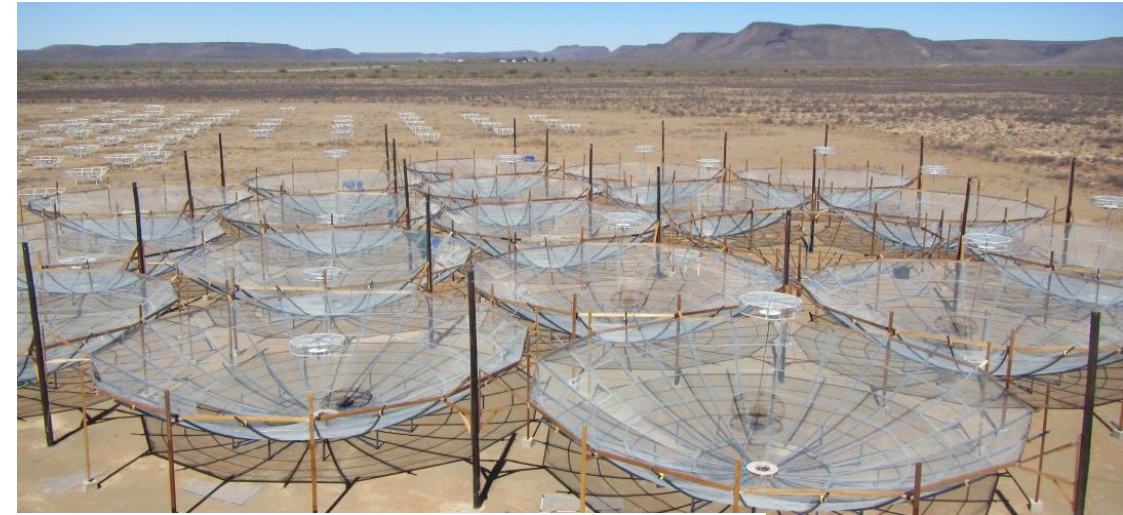
- Delta-function-like PDF
- Positive skewness
- Positive kurtosis



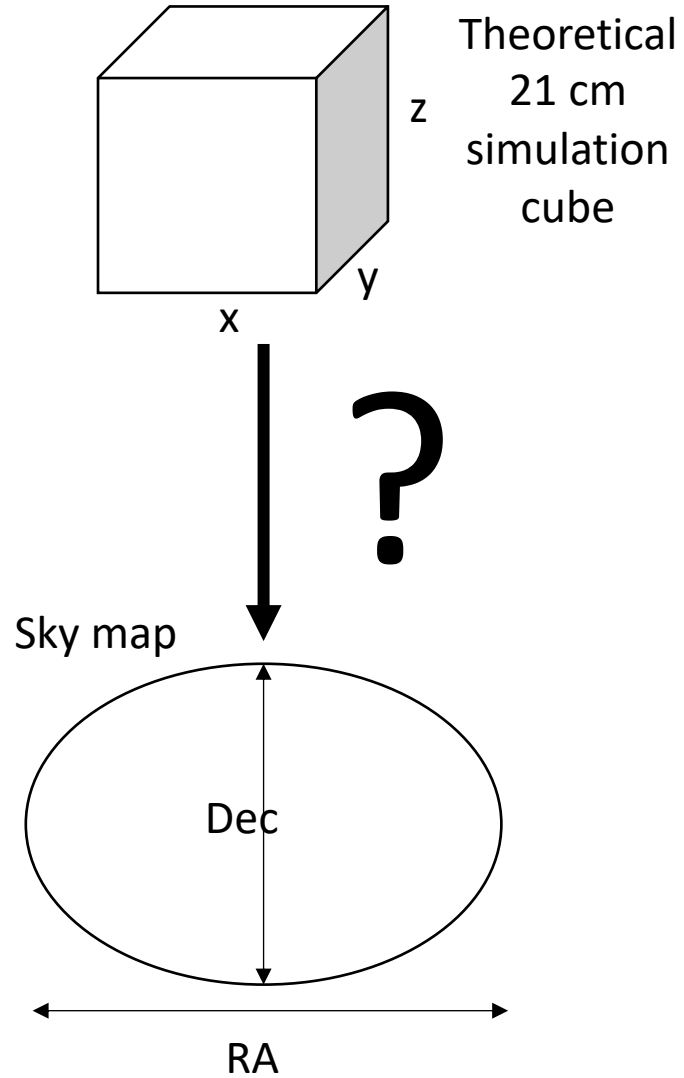


# Sensitivity Analysis of 21 cm One-point Statistics for HERA

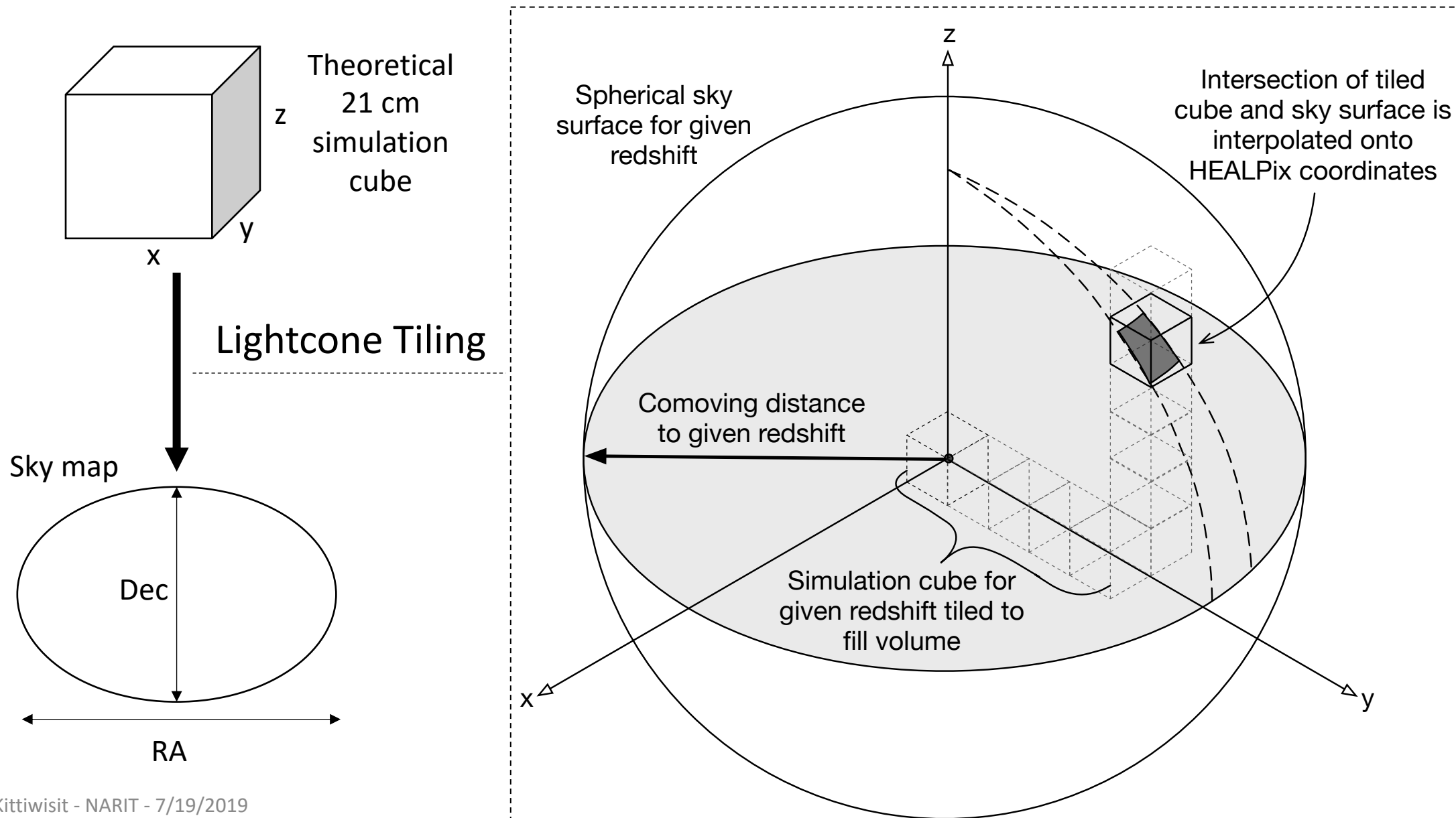
- Utilize realistic mock observation pipeline
  - Variance, skewness and kurtosis
  - Full-sky 21 cm inputs
  - HERA as the instrument model
  - Thermal noise
  - Sample variance
  - Drift scan observation
  - Frequency bandwidth averaging
  - Assume perfect foreground removal and foreground avoiding regimes
- Kittiwisit et al. 2018, MNRAS, arXiv:1708.00036



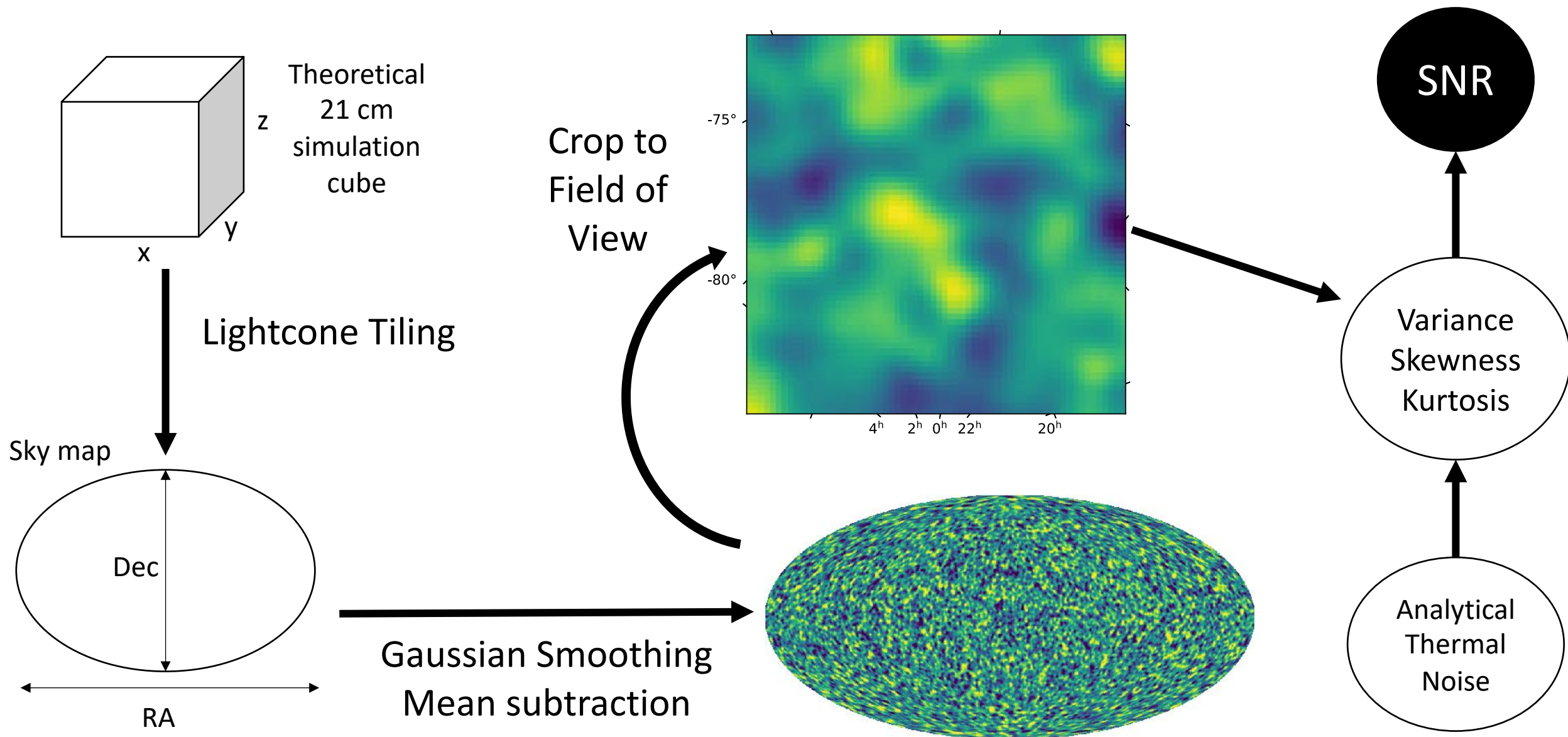
# HERA Mock Observation Pipeline (No Foreground)



# HERA Mock Observation Pipeline (No Foreground)

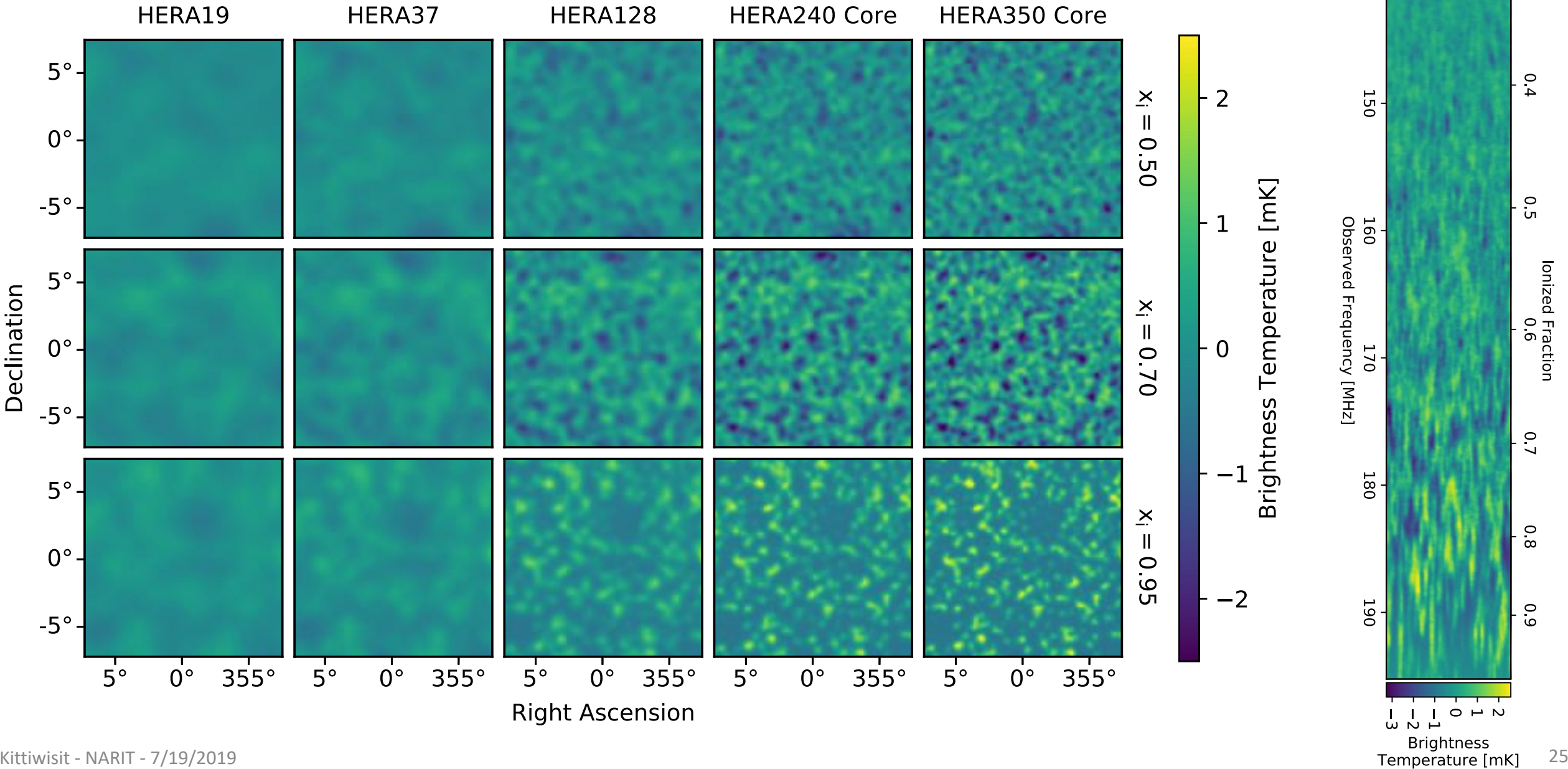


# HERA Mock Observation Pipeline (No Foreground)



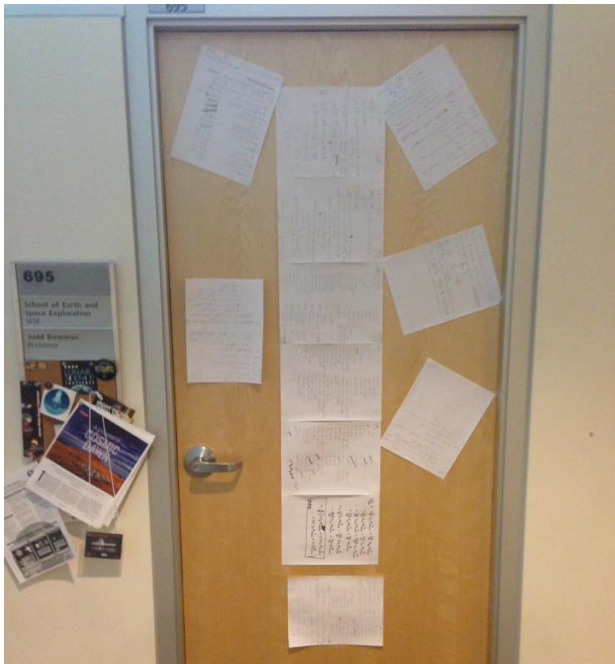


# Simulated Intensity Maps



# Analytical Thermal Noise Uncertainty

- Expanded from Watkinson & Pritchard 2014 to kurtosis
- 100 hours of integration, approximately 1 year



$\langle n_i \rangle$	$= 0$	
$\langle n_i n_j \rangle$	$\langle n_i^2 \rangle = \sigma_i^2 \quad (i = j)$ $\langle n_i \rangle \langle n_j \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i n_j \rangle} \right\} \delta_{ij} \sigma_j^2$
$\langle n_i n_j^2 \rangle$	$\langle n_i^3 \rangle = 0 \quad (i = j)$ $\langle n_i \rangle \langle n_j^2 \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i n_j^2 \rangle} \right\} 0$
$\langle n_i^2 n_j^2 \rangle$	$\langle n_i^4 \rangle = 3\sigma_i^4 \quad (i = j)$ $\langle n_i^2 \rangle \langle n_j^2 \rangle = \sigma_i^2 \sigma_j^2 \quad (i \neq j)$	$\left. \vphantom{\langle n_i^2 n_j^2 \rangle} \right\} (1 + 2\delta_{ij}) \sigma_i^2 \sigma_j^2$
$\langle n_i^2 n_j^3 \rangle$	$\langle n_i^5 \rangle = 0 \quad (i = j)$ $\langle n_i^2 \rangle \langle n_j^3 \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i^2 n_j^3 \rangle} \right\} 0$
$\langle n_i n_j^3 \rangle$	$\langle n_i^4 \rangle = 3\sigma_i^4 \quad (i = j)$ $\langle n_i \rangle \langle n_j^3 \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i n_j^3 \rangle} \right\} 3\delta_{ij} \sigma_i^4$
$\langle n_i^3 n_j^3 \rangle$	$\langle n_i^6 \rangle = 15\sigma_i^6 \quad (i = j)$ $\langle n_i^3 \rangle \langle n_j^3 \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i^3 n_j^3 \rangle} \right\} 15\delta_{ij} \sigma_i^6$
$\langle n_i n_j^4 \rangle$	$\langle n_i^5 \rangle = 0 \quad (i = j)$ $\langle n_i \rangle \langle n_j^4 \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i n_j^4 \rangle} \right\} 0$
$\langle n_i^2 n_j^4 \rangle$	$\langle n_i^6 \rangle = 15\sigma_i^6 \quad (i = j)$ $\langle n_i^2 \rangle \langle n_j^4 \rangle = 3\sigma_i^2 \sigma_j^4 \quad (i \neq j)$	$\left. \vphantom{\langle n_i^2 n_j^4 \rangle} \right\} (3 + 12\delta_{ij}) \sigma_i^2 \sigma_j^4$
$\langle n_i^3 n_j^4 \rangle$	$\langle n_i^7 \rangle = 0 \quad (i = j)$ $\langle n_i^3 \rangle \langle n_j^4 \rangle = 0 \quad (i \neq j)$	$\left. \vphantom{\langle n_i^3 n_j^4 \rangle} \right\} 0$
$\langle n_i^4 n_j^4 \rangle$	$\langle n_i^8 \rangle = 105\sigma_i^8 \quad (i = j)$ $\langle n_i^4 \rangle \langle n_j^4 \rangle = 9\sigma_i^4 \sigma_j^4 \quad (i \neq j)$	$\left. \vphantom{\langle n_i^4 n_j^4 \rangle} \right\} (9 + 96\delta_{ij}) \sigma_i^4 \sigma_j^4$

skewness, and  $X = m_2$  and  $Y = m_4$  for kurtosis.

Equations A9 to A14 summarize results from Watkinson & Pritchard (2014). Here,  $\sigma_i$  is assumed to be equal to  $\sigma_{noise}$  in Equation 7 for all pixels.

$$\hat{m}_2 = \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^2 - \sigma_{noise}^2, \quad (A9)$$

$$\hat{m}_3 = \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^3, \quad (A10)$$

$$C_{\hat{m}_2 \hat{m}_3} = \frac{6}{N_{pix}} m_3 \sigma_{noise}^2, \quad (A11)$$

$$V_{\hat{m}_2} = V_{Var} = \frac{2}{N_{pix}} (2m_2 \sigma_{noise}^2 + \sigma_{noise}^4), \quad (A12)$$

$$V_{\hat{m}_3} = \frac{3}{N_{pix}} (3m_4 \sigma_{noise}^2 + 12m_2 \sigma_{noise}^4 + 5\sigma_{noise}^6), \quad (A13)$$

$$V_{S_3} \approx \frac{1}{(m_2)^3} V_{\hat{m}_3} + \frac{9}{4} \frac{(m_3)^2}{(m_2)^5} V_{\hat{m}_2} - 3 \frac{m_3}{(m_2)^4} C_{\hat{m}_2 \hat{m}_3}. \quad (A14)$$

We follow the procedure in Watkinson & Pritchard (2014) and are able to confirm their results. In addition, we derive the estimator variance for kurtosis as follows.

First the 4th moment with added noise is constructed.

$$\begin{aligned} \hat{m}_4^{(est)} &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (x_i - \bar{x})^4 \\ &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} [(\delta T_i - \bar{\delta T}) + n_i]^4. \end{aligned} \quad (A15)$$

Then, we average over the noise.

$$\begin{aligned} \langle \hat{m}_4^{(est)} \rangle &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} [(\delta T_i - \bar{\delta T})^4 + 4(\delta T_i - \bar{\delta T})^3 \langle n_i \rangle \\ &\quad + 6(\delta T_i - \bar{\delta T})^2 \langle n_i^2 \rangle + 4(\delta T_i - \bar{\delta T}) \langle n_i^3 \rangle + \langle n_i^4 \rangle] \\ &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^4 \\ &\quad + 6 \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^2 \sigma_i^2 + 3\sigma_i^4 \\ &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^4 \\ &\quad + 6m_2 \sigma_{noise}^2 + 3\sigma_{noise}^4. \end{aligned} \quad (A16)$$

This implies that the unbiased estimator of the 4th moment is,

$$\begin{aligned} \hat{m}_4 &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^4 - 6m_2 \sigma_{noise}^2 - 3\sigma_{noise}^4 \\ &= \frac{1}{N_{pix}} \sum_{i=0}^{N_{pix}} (\delta T_i - \bar{\delta T})^4 - \frac{3}{2} N_{pix} V_{\hat{m}_2}. \end{aligned} \quad (A17)$$

Next we derive the estimator variance of the 4th moment. We substitute  $\mu_i = \delta T_i - \bar{\delta T}$  and  $\kappa = 3N_{pix} V_{\hat{m}_2} / 2$  to simplify the derivation.

$$\begin{aligned} V_{\hat{m}_4} &= \left\langle \frac{1}{N_{pix}^2} \sum_{i=0}^{N_{pix}} \sum_{j=0}^{N_{pix}} [(\mu_i + n_i)^4 - \kappa] \right. \\ &\quad \left. \times [(\mu_j + n_j)^4 - \kappa] \right\rangle - (m_4)^2. \end{aligned} \quad (A18)$$

Expanding this expression and moving the noise averaging brackets inside the summation gives,

$$\begin{aligned} V_{\hat{m}_4} &= \frac{1}{N_{pix}^2} \sum_{i=0}^{N_{pix}} \sum_{j=0}^{N_{pix}} [\mu_i^4 \mu_j^4 + 4\mu_i^4 \mu_j^3 \langle n_j \rangle \\ &\quad + 6\mu_i^4 \mu_j^2 \langle n_j^2 \rangle + 4\mu_i^4 \mu_j \langle n_j^3 \rangle + \mu_i^4 \langle n_j^4 \rangle - \kappa \mu_i^4 \\ &\quad + 4\mu_i^3 \mu_j^4 \langle n_i \rangle + 16\mu_i^3 \mu_j^3 \langle n_i n_j \rangle + 24\mu_i^3 \mu_j^2 \langle n_i n_j^2 \rangle \\ &\quad + 16\mu_i^3 \mu_j \langle n_i n_j^3 \rangle + 4\mu_i^3 \langle n_i n_j^4 \rangle - 4\kappa \mu_i^3 \langle n_i \rangle \\ &\quad + 6\mu_i^2 \mu_j^4 \langle n_i^2 \rangle + 24\mu_i^2 \mu_j^3 \langle n_i^2 n_j \rangle + 36\mu_i^2 \mu_j^2 \langle n_i^2 n_j^2 \rangle \\ &\quad + 24\mu_i^2 \mu_j \langle n_i^2 n_j^3 \rangle + 6\mu_i^2 \langle n_i^2 n_j^4 \rangle - 6\kappa \mu_i^2 \langle n_i^2 \rangle \\ &\quad + 4\mu_i \mu_j^4 \langle n_i^3 \rangle + 16\mu_i \mu_j^3 \langle n_i^3 n_j \rangle + 24\mu_i \mu_j^2 \langle n_i^3 n_j^2 \rangle \\ &\quad + 16\mu_i \mu_j \langle n_i^3 n_j^3 \rangle + 4\mu_i \langle n_i^3 n_j^4 \rangle - 4\kappa \mu_i \langle n_i^3 \rangle \\ &\quad + \mu_i^4 \langle n_i^4 \rangle + 4\mu_i^3 \langle n_i^4 n_j \rangle + 6\mu_i^2 \langle n_i^4 n_j^2 \rangle \\ &\quad + 4\mu_j \langle n_j^4 n_i^3 \rangle + \langle n_i^4 n_j^4 \rangle - \kappa \langle n_i^4 \rangle \\ &\quad - \kappa \mu_j^4 - 4\kappa \mu_j^3 \langle n_j \rangle - 6\kappa \mu_j^2 \langle n_j^2 \rangle - 4\kappa \mu_j \langle n_j^3 \rangle \\ &\quad - \kappa \langle n_j^4 \rangle + \kappa^2] - (m_4)^2. \end{aligned} \quad (A19)$$

Using the Gaussian noise identities reduces the expression to,

$$\begin{aligned} V_{\hat{m}_4} &= \frac{1}{N_{pix}^2} \sum_{i=0}^{N_{pix}} \sum_{j=0}^{N_{pix}} [\mu_i^4 \mu_j^4 + 6\mu_i^4 \mu_j^2 \sigma_j^2 + 3\mu_i^4 \sigma_j^4 - \kappa \mu_i^4 \\ &\quad + 16\mu_i^3 \mu_j^3 \delta_{ij} \sigma_j^2 + 48\mu_i^3 \mu_j \delta_{ij} \sigma_j^4 + 6\mu_i^2 \mu_j^2 \sigma_i^2 \\ &\quad + 36\mu_i^2 \mu_j^2 (1 + 2\delta_{ij}) \sigma_i^2 \sigma_j^2 + 6\mu_i^2 (3 + 12\delta_{ij}) \sigma_i^2 \sigma_j^4 \\ &\quad - 6\kappa \mu_i^2 \sigma_i^2 + 48\mu_i \mu_j^3 \delta_{ij} \sigma_j^4 + 240\mu_i \mu_j \delta_{ij} \sigma_i^6 \\ &\quad + 3\mu_i^4 \sigma_i^4 + 6\mu_i^2 (3 + 12\delta_{ij}) \sigma_i^4 \sigma_j^2 + (9 + 96\delta_{ij}) \sigma_i^4 \sigma_j^4 \\ &\quad - 3\kappa \sigma_i^4 - \kappa \mu_j^4 - 6\kappa \mu_j^2 \sigma_j^2 - 3\kappa \sigma_j^4 + \kappa^2] \\ &\quad - (m_4)^2. \end{aligned} \quad (A20)$$

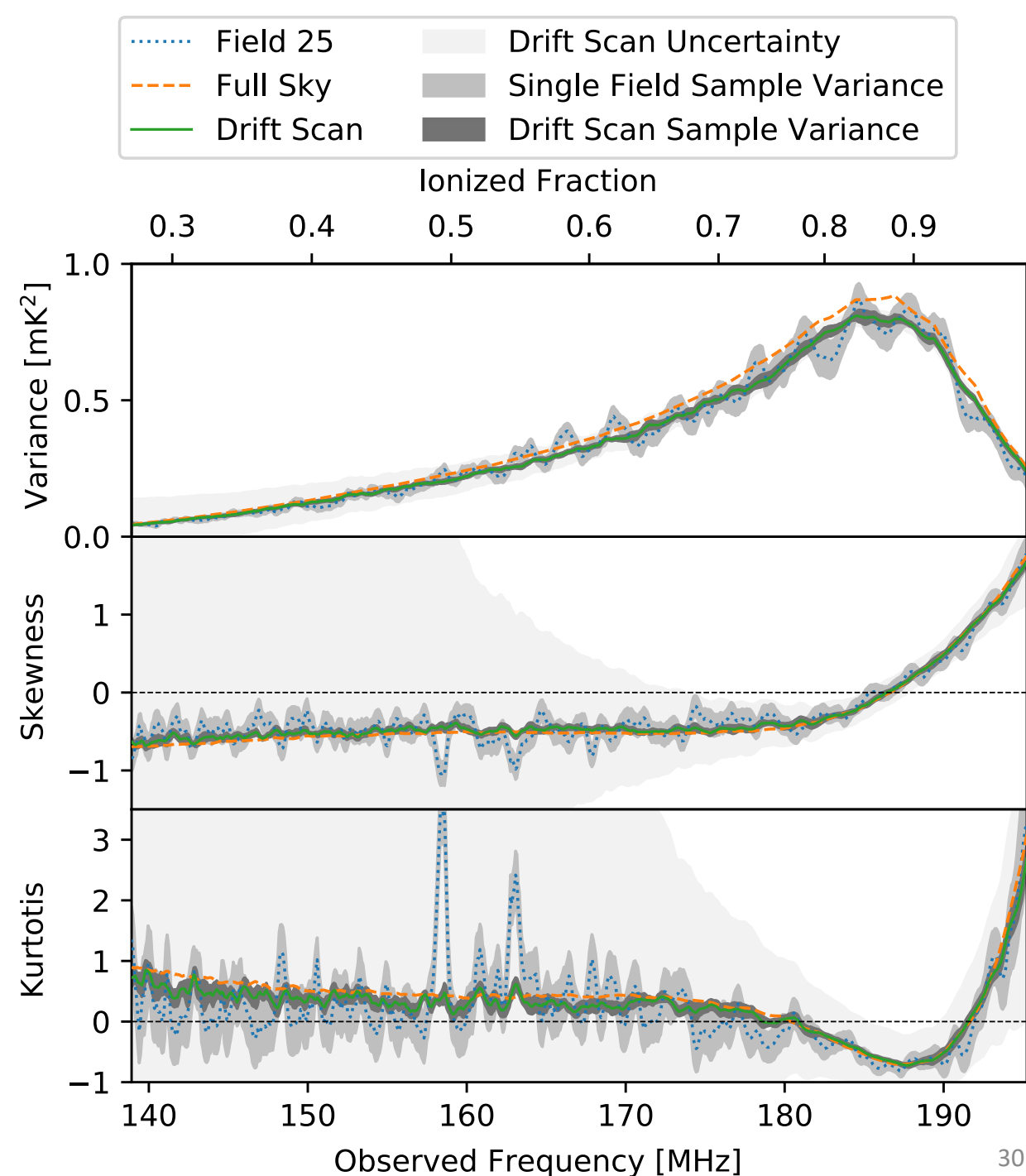
Doing the summation to perform index conversion via  $\delta_{ij}$ , substituting all  $\frac{1}{N_{pix}^2} \sum_{i=0}^{N_{pix}} \sum_{j=0}^{N_{pix}} \mu_i^4$  terms with the p-th moments  $m_p$  and  $\sigma_i$  with  $\sigma_{noise}$ , re-substituting  $\kappa = 3N_{pix} V_{\hat{m}_2} / 2 = 6m_2 \sigma_{noise}^2 + 3\sigma_{noise}^4$ , and cancelling out many terms will yield the estimator variance of the 4th moment,

$$V_{\hat{m}_4} = \frac{8}{N_{pix}} (2m_6 \sigma_{noise}^2 + 21m_4 \sigma_{noise}^4 + 48m_2 \sigma_{noise}^6 + 12\sigma_{noise}^8). \quad (A21)$$

The estimator covariance between 2nd and 4th moment

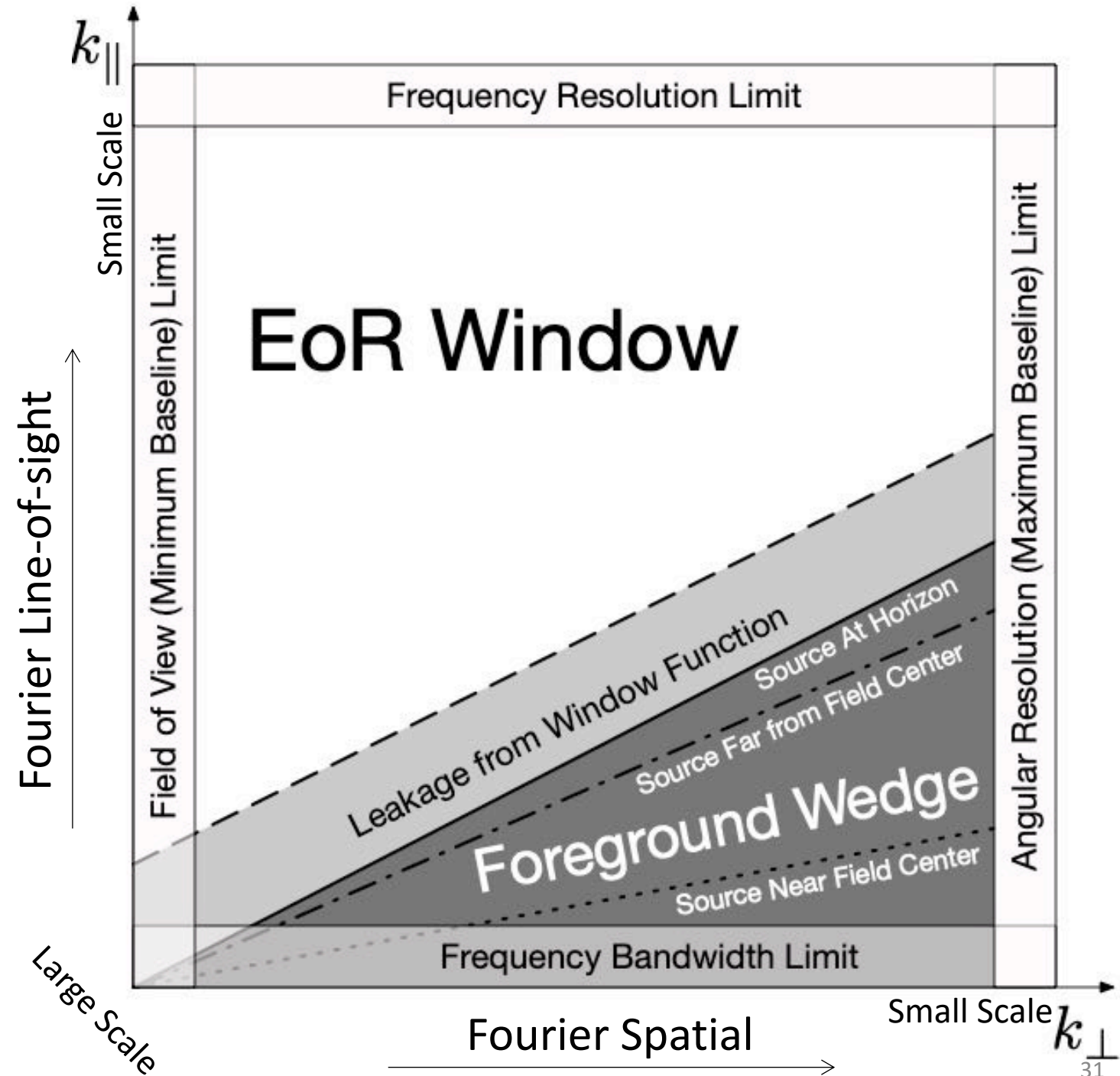
# HERA350 Core Measurement (80 kHz channel, 1 year noise)

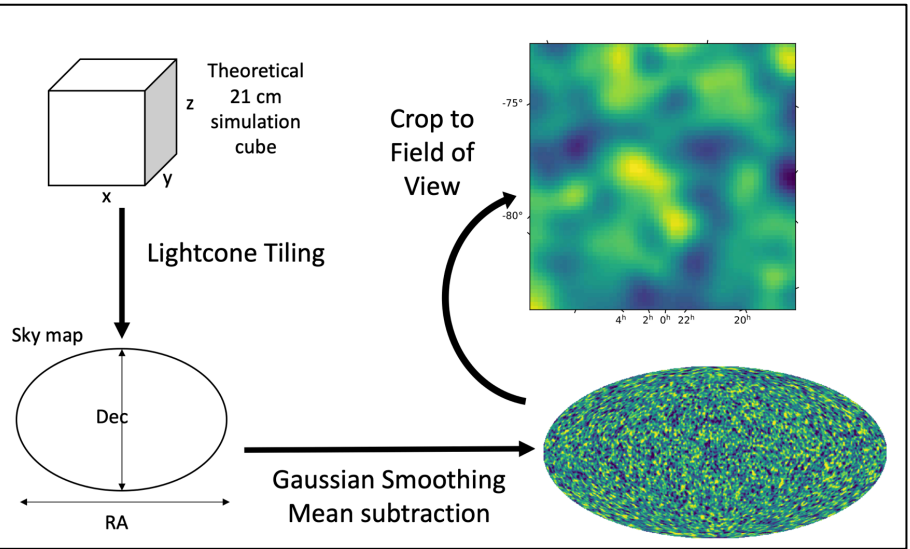
- Strong fluctuations in measurements from a single field due to sample variance
- Averaging over 20 measurements from different fields in the HERA drift scan recovers statistics of the sky model
- Thermal noise dominate skewness and kurtosis at low frequency
  - But measurements are possible at higher frequency (where it matters)



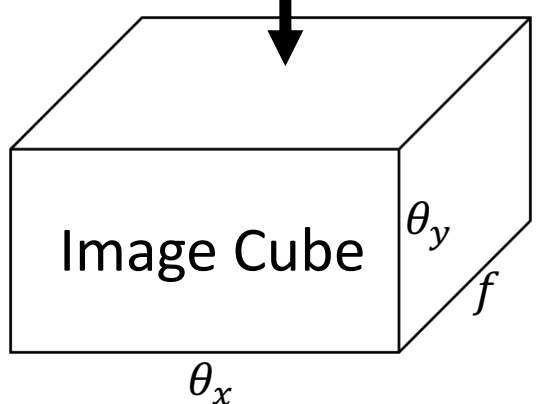
# How to Deal with Foreground?

- Subtracting foreground is hard to do
- “Avoiding” foreground is easier to do
- Foreground is contained in a wedge-shape region in the 2D Fourier space
- See, e.g., Morales et al., ApJ, 752, 2, (2012)

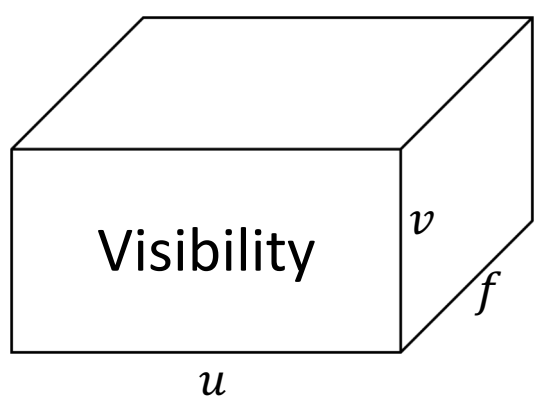




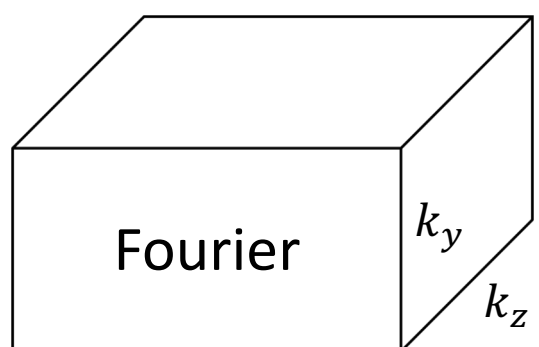
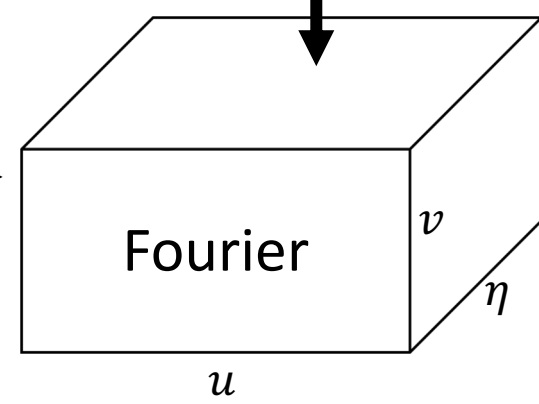
Repeat for Every Frequency



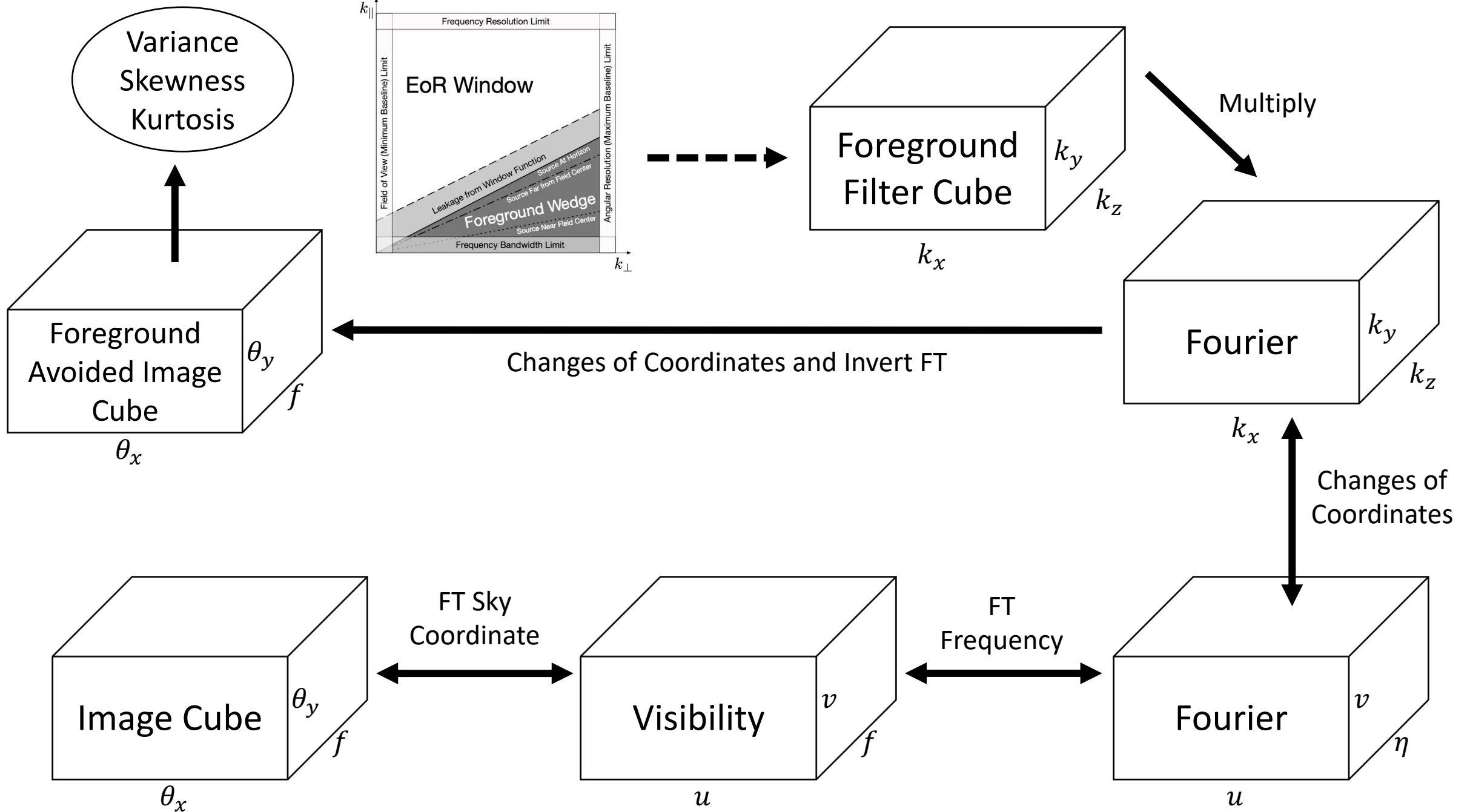
FT Sky Coordinate

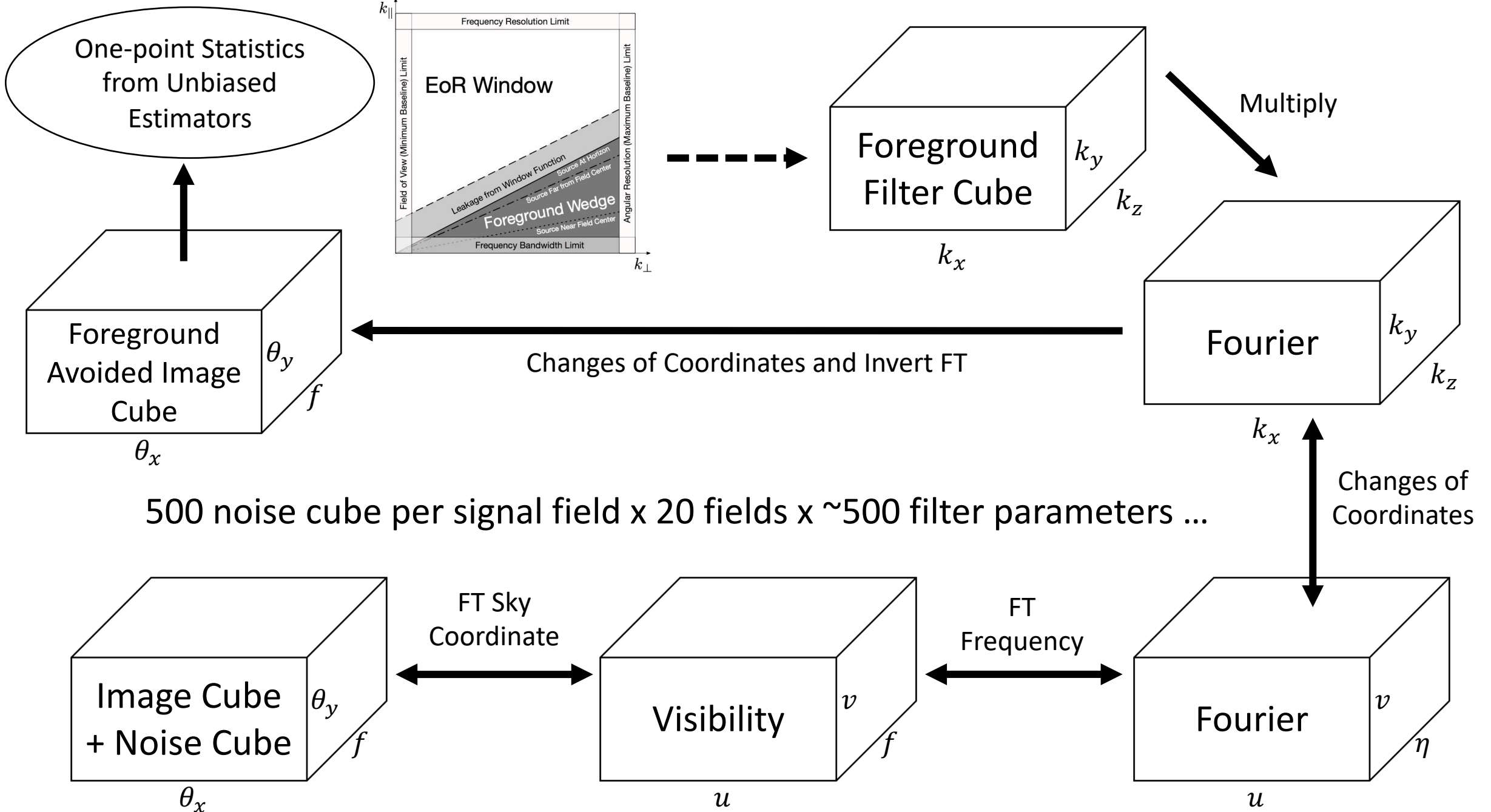


FT Frequency



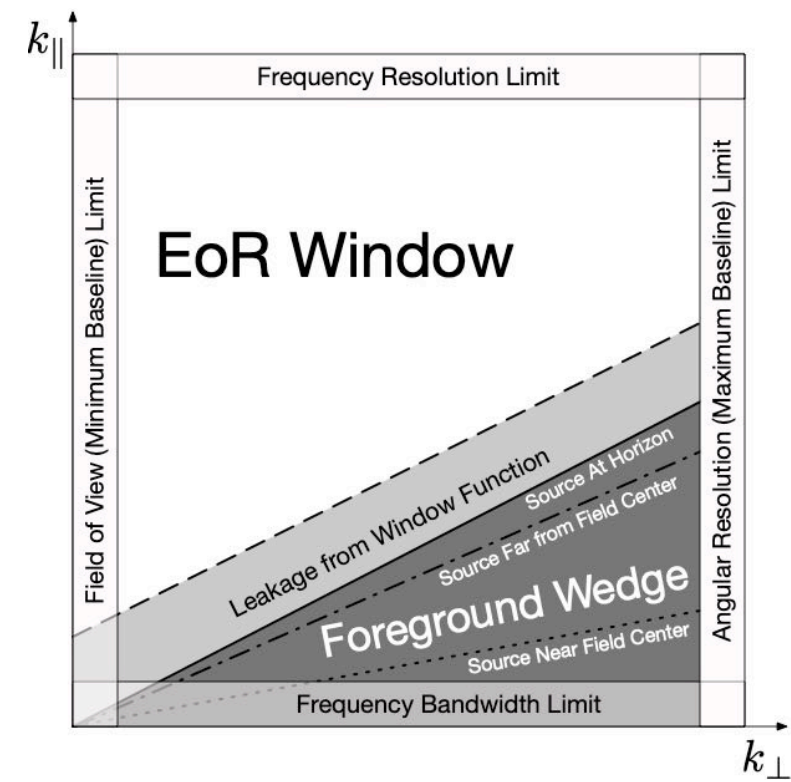
Changes of Coordinates





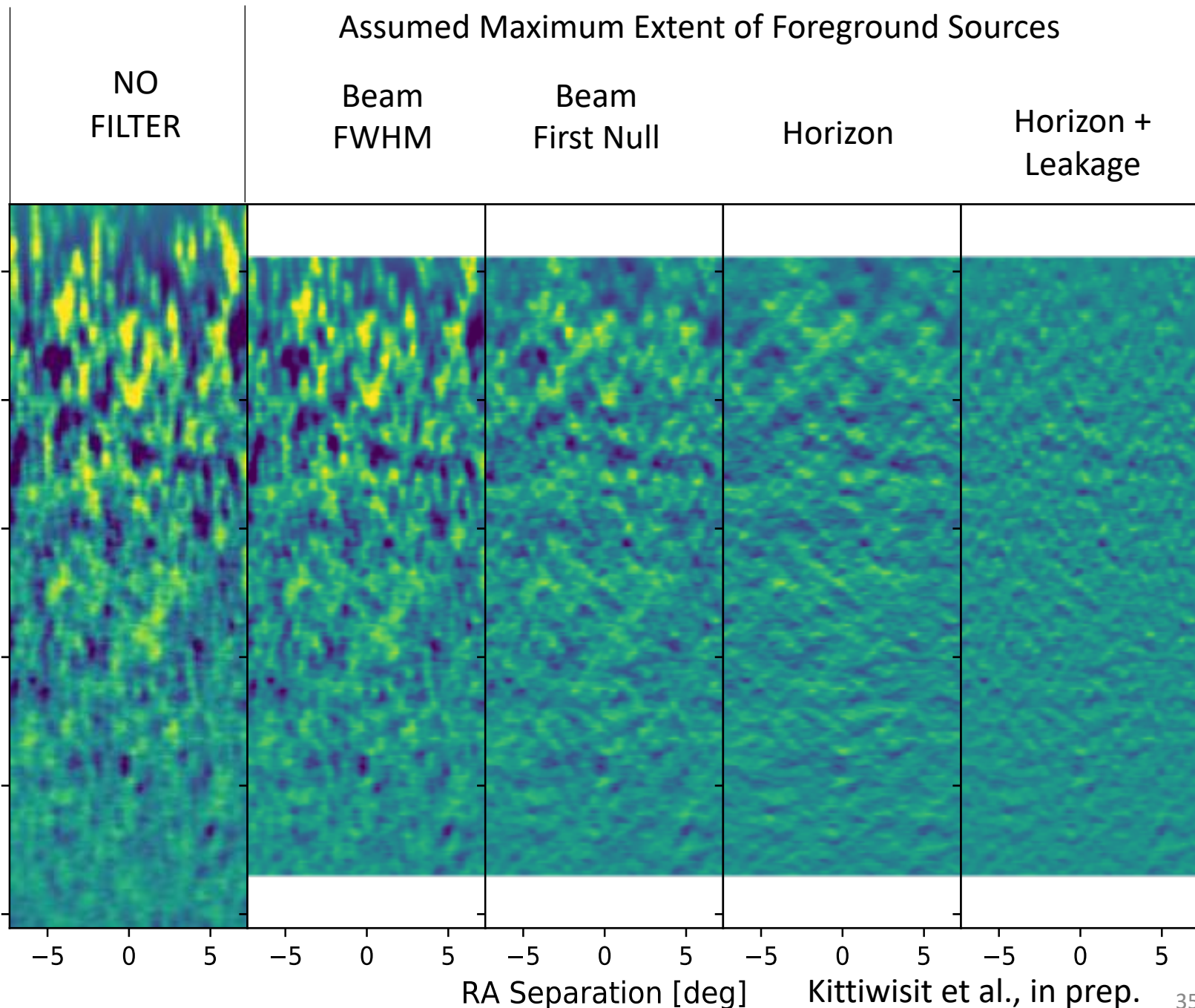
# Foreground Avoided Intensity Maps

- 8-MHz Rolling Filter
- HERA350



Observed Frequency [MHz]

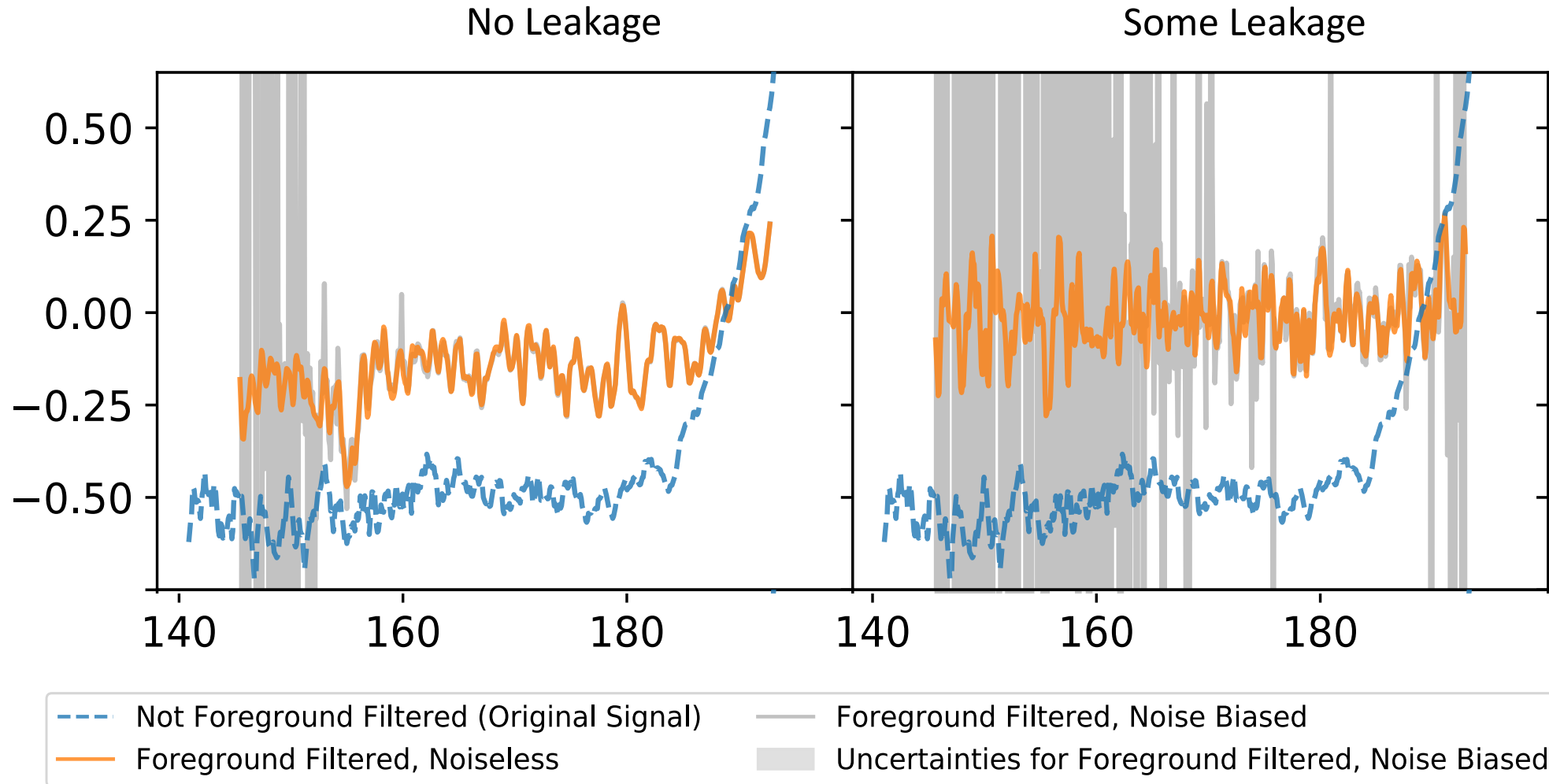
190  
180  
170  
160  
150  
140





# Prediction for HERA - Foreground Avoidance Regime

- 1 MHz channel, 2 year integration
- Need to control leakage from Fourier transform (or integrate much longer)

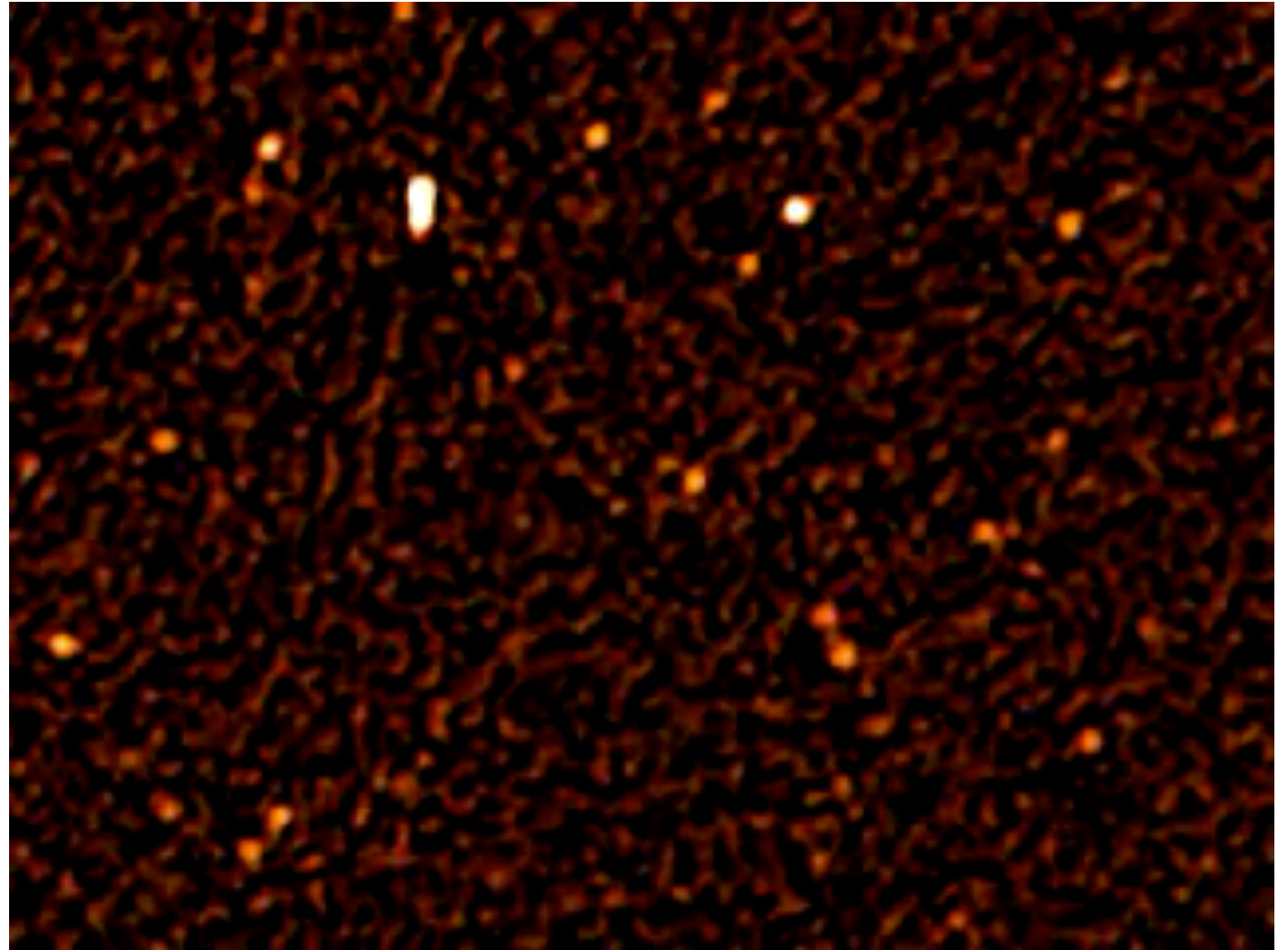


# Part II – Summary

- One-point statistics of 21 cm signal
  - Describe the shape of the PDF of 21 cm fluctuations
  - Check for non-Gaussianity in reionization
  - Infer different phases of reionization
  - Distinguish different reionization model (e.g., Watkinson et al. 2014)
- Can HERA measure 21 cm one-point statistics?
  - Yes, if we can mitigate the foreground
  - In the foreground avoidance regime, we need to control spectral leakage
  - We need to explore foreground subtraction regime
  - What kind of reionization physics can we infer?

# Ionospheric Study with Low-frequency Radio Array

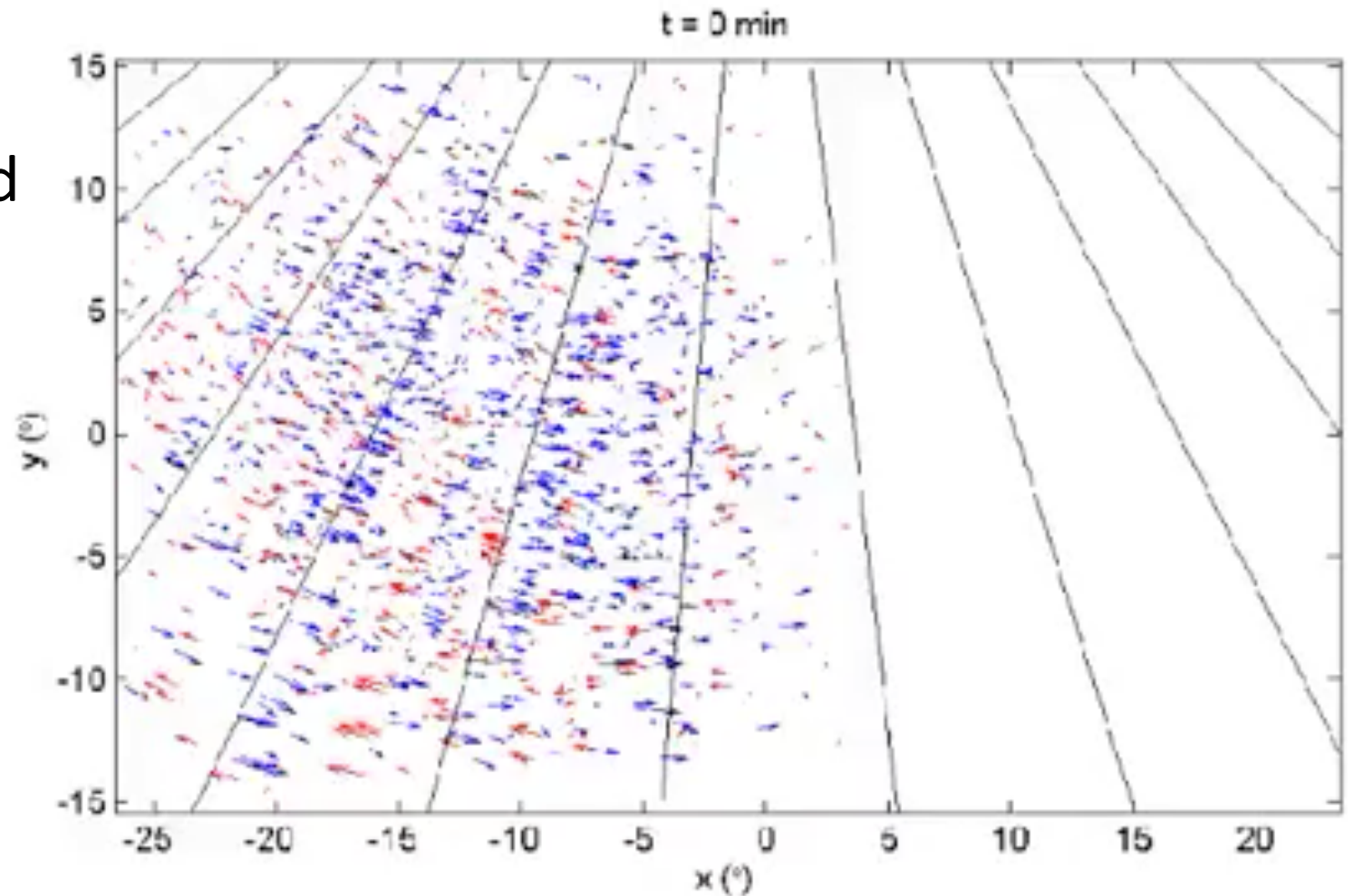
- Anisotropic plasma density affects incoming foreground wavefronts and must be corrected in EoR analysis.



See <https://youtu.be/5KWGDx0fq50> for the movie version of the figure

# Ionospheric Study with Low-frequency Radio Array

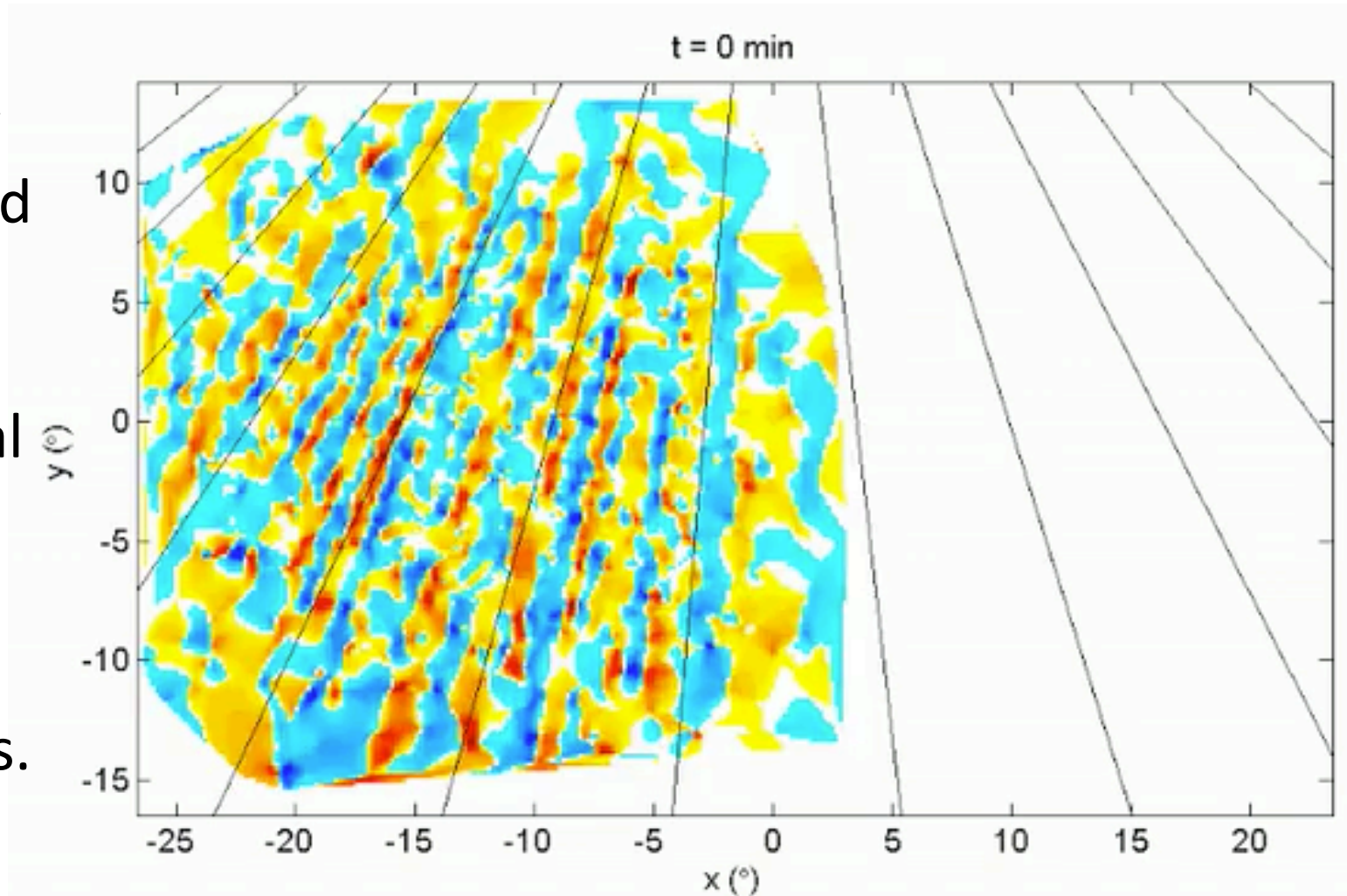
- Anisotropic plasma density affects incoming foreground wavefronts and must be corrected in EoR analysis.
- Loi et al. 2016, Geophysical Research Letters, probed the plasma movements in the MWA data sets.



See <https://youtu.be/rYXuZsNWGmg> for the movie version of the figure

# Ionospheric Study with Low-frequency Radio Array

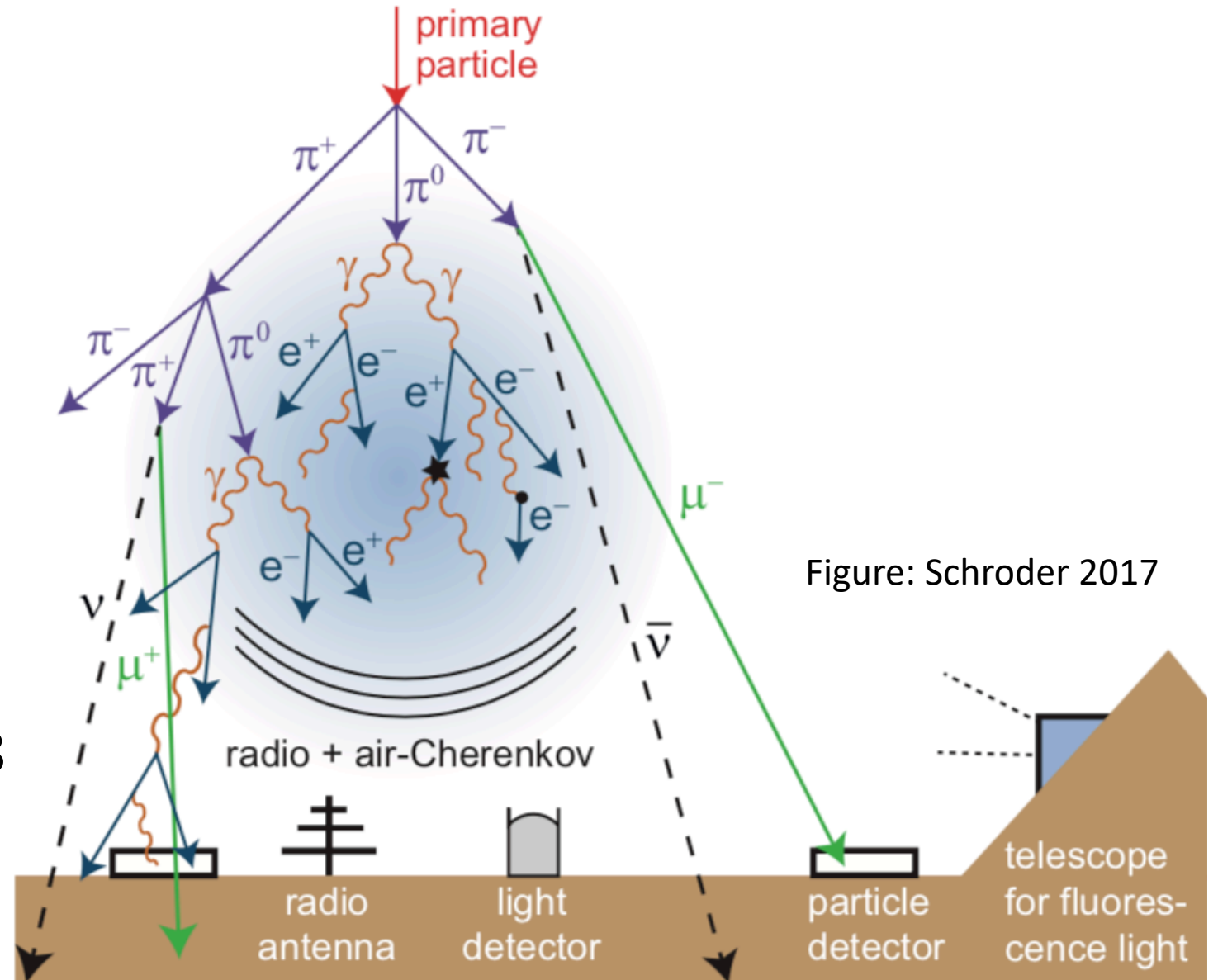
- Anisotropic plasma density affects incoming foreground wavefronts and must be corrected in EoR analysis.
- Loi et al., 2016, Geophysical Research Letters, probed the plasma movements in the MWA data sets and visualized the plasma tubes.
- See Jordan et al., 2017 and Trott et al., 2018 for recent application to EoR analysis.



See <https://youtu.be/-A3YjUL9JAI> for the movie version of the figure

# Radio Detection of Cosmic Ray Air Showers

- Deploy scintillator to trigger and confirm radio detection of cosmic-rays
  - LOFAR Radboud Air Shower Array (see Buitink et al. 2017, Nature)
- Or self-triggered
  - Demonstrated by LWA-OWVR
  - GRAND (<http://grand.cnrs.fr/>)
- See Schroder 2017, Prog.Part.Nucl.Phys., 93, 1-68 for recent review



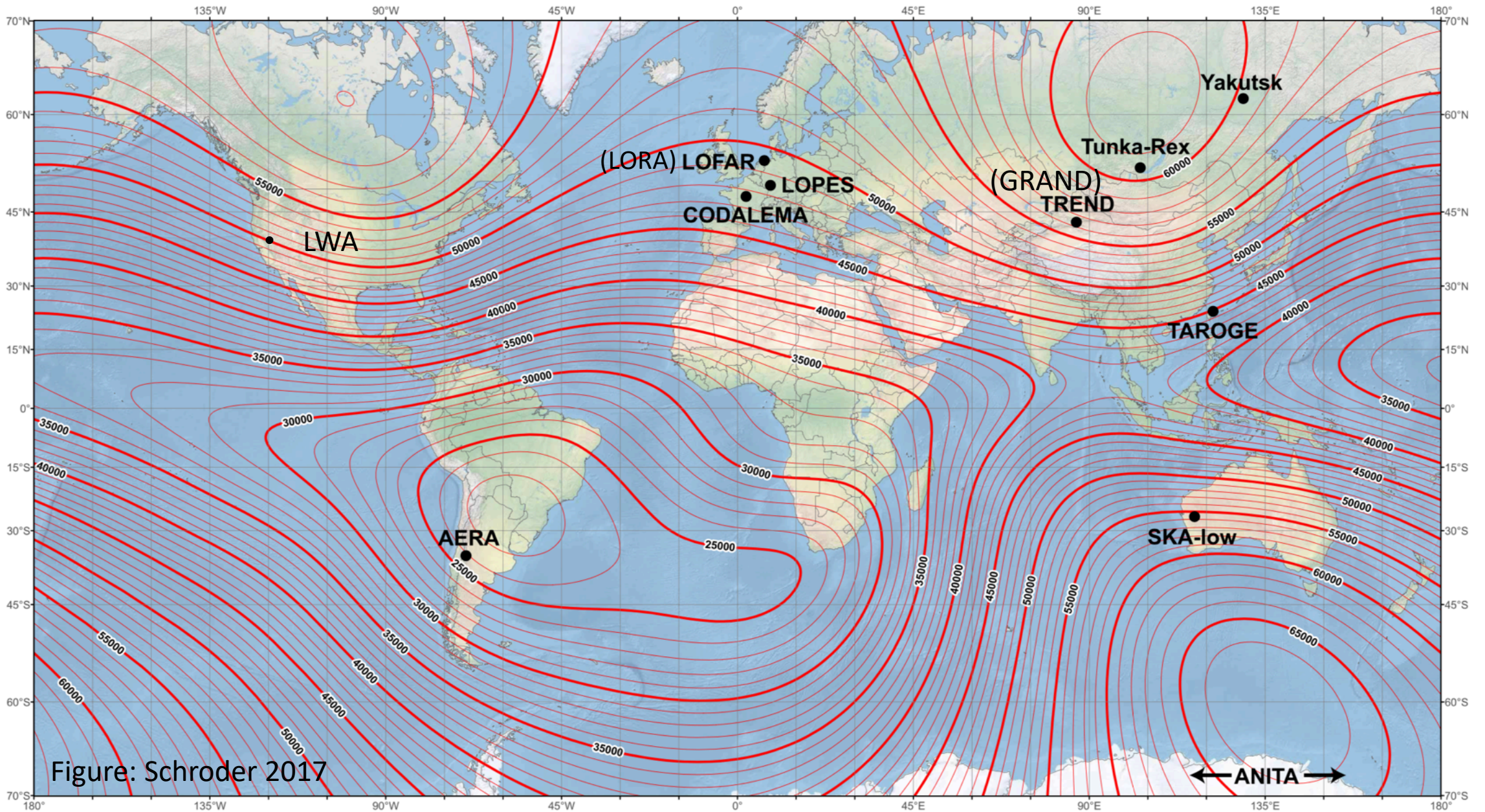


Figure: Schroder 2017

Underlying map (Mercator projection):  
 Main Geomagnetic Field Total Intensity with contour intervals of 1000 nT  
 according to US/UK World Magnetic Model - Epoch 2015.0

developed by NOAA/NGDC & CIRES  
<http://ngdc.noaa.gov/geomag/WMM>

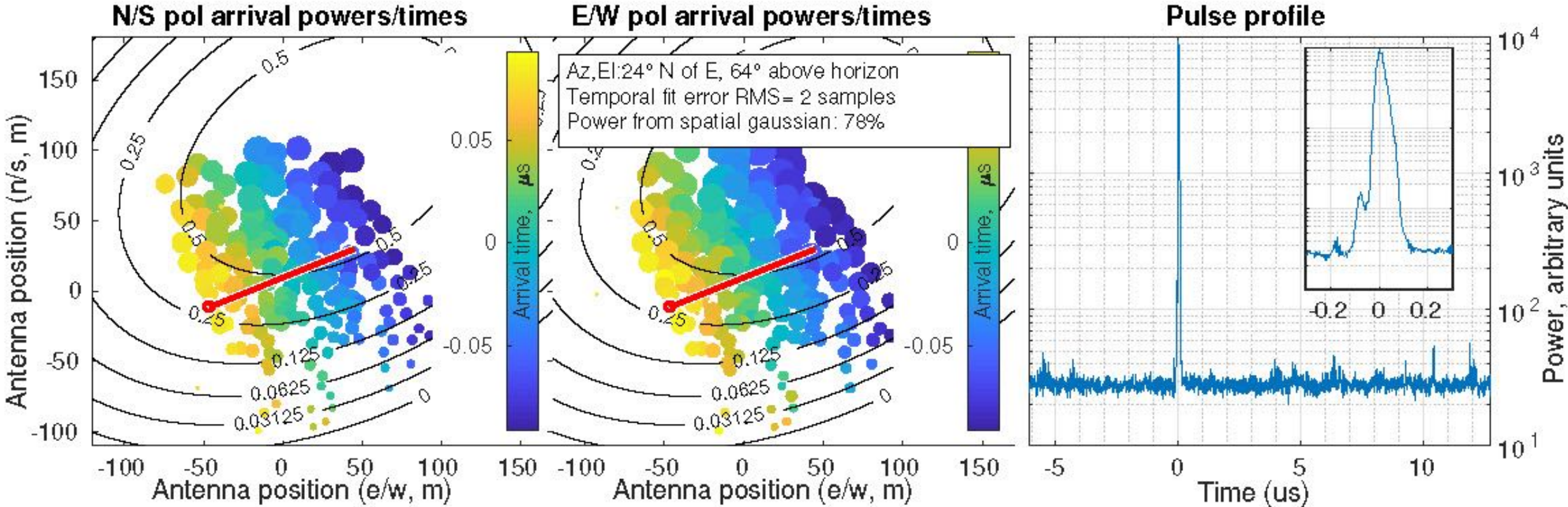
Map reviewed by NGA and BGS  
 Published December 2014

Overlaid: Location of radio experiments for cosmic-ray air showers  
 added on underlying map by Frank G. Schröder  
 Karlsruhe Institute of Technology (KIT), Germany

# Self-triggered Detection at the Owens Valley Long Wavelength Array



Credit: Monroe's Thesis, Caltech, 2018





# Conclusion

- Low-frequency radio observations are exciting new frontiers for cosmology, astrophysics, ionospheric sciences, particle physics, and beyond
- Challenging due to complication from complex instruments and requirements for data processing
- Reionization and Cosmic Dawn is the main driver, but other science cases are as exciting